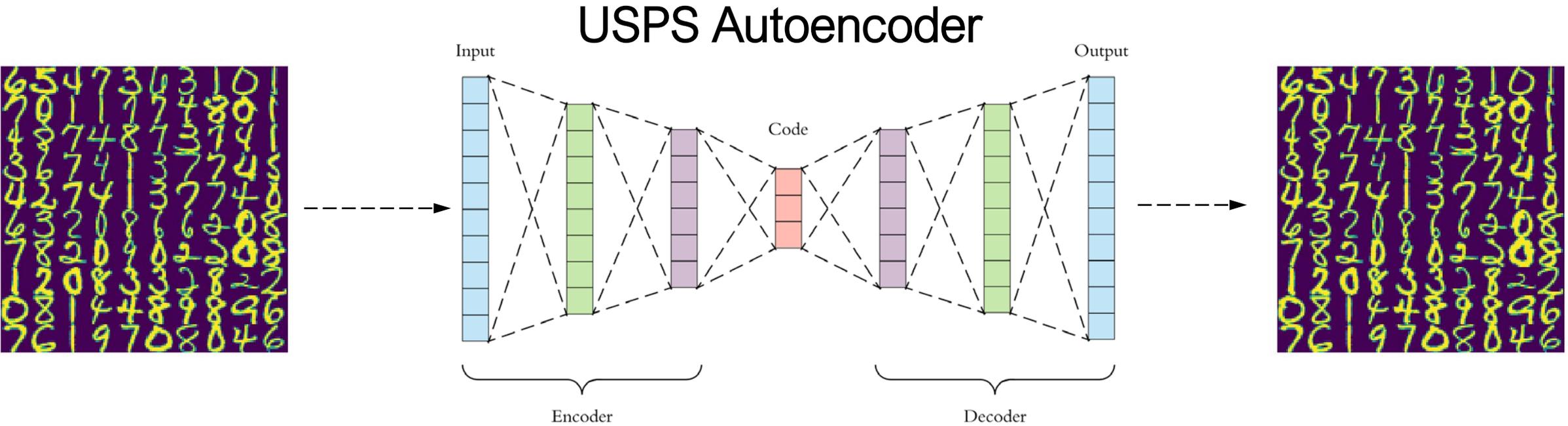


# Robust Projection onto Image Manifolds

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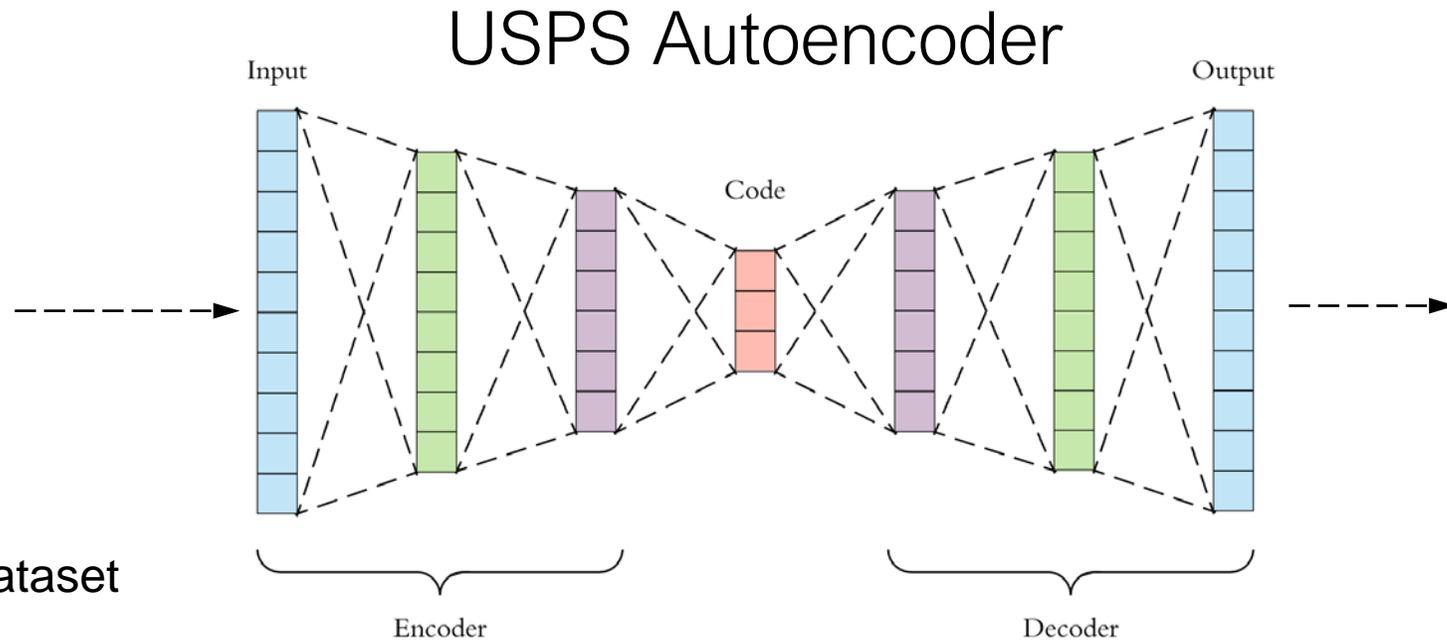
# Motivation



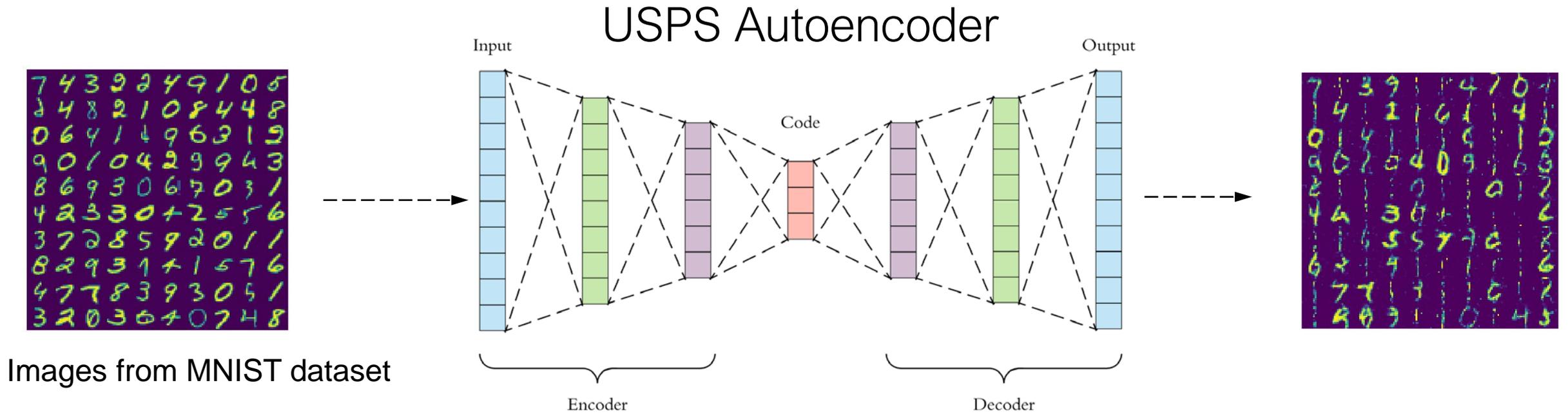
# Reconstructing when dataset has changed?



Images from MNIST dataset



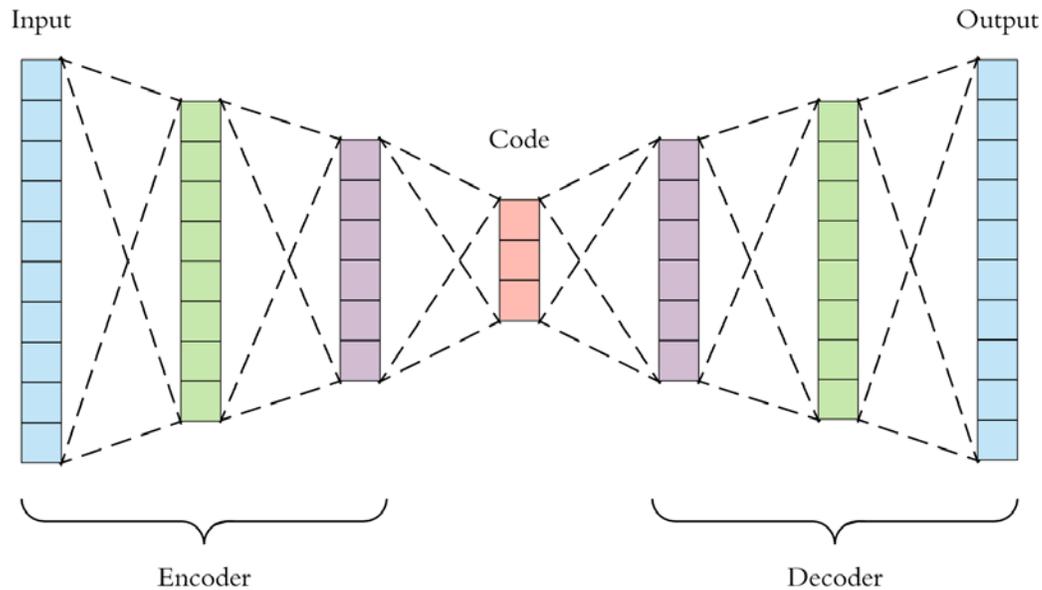
# Reconstructing when dataset has changed?



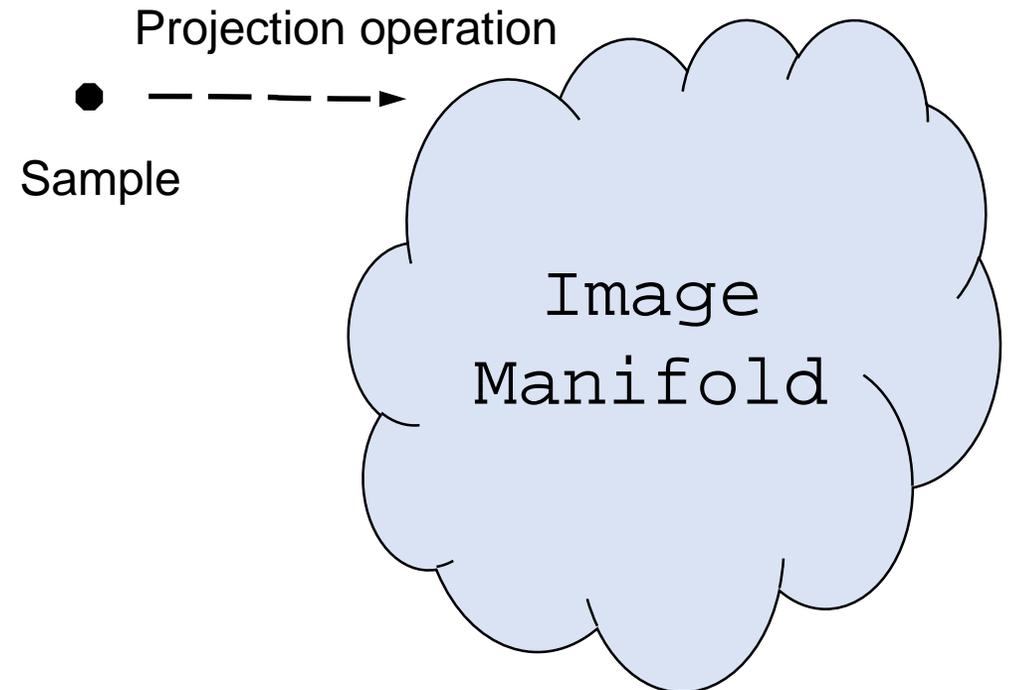
Autoencoder cannot handle the distribution shift

# Projection 101: How do we project onto a manifold?

*A: Encoder + decoder model  
(direct inference)*



*B: Extrinsic Mapping onto the manifold  
(in-direct inference)*



# In-direct inference: PGD optimization

Final projection is given by  $\mathcal{G}(z^*)$

$$z^* = \arg \min_{z \in \mathbb{R}^d} \|Y - \mathcal{G}(z^*)\|$$

Minimize decoder output

Projected Gradient Descent: Walking in the latent space to minimize projection error

# Why is it not robust?

Take a simple example where the image to be projected is corrupted in an unknown fashion:

$$Y \rightarrow \mathcal{F}^?(Y)$$

$$z^* = \arg \min_{z \in \mathbb{R}^d} \|\mathcal{F}^?(Y) - \mathcal{G}(z)\|$$

Unless the loss function is robust to the corruption “F”, **this optimization will fail.**



Examples from the face manifold

$\mathcal{F}^?(Y)$



Corrupted observations with no knowledge of corruption

$\mathcal{G}(z^*)$



# How do we make it more Robust?

The unknown corruption is causing the issue, so we can try to estimate it.

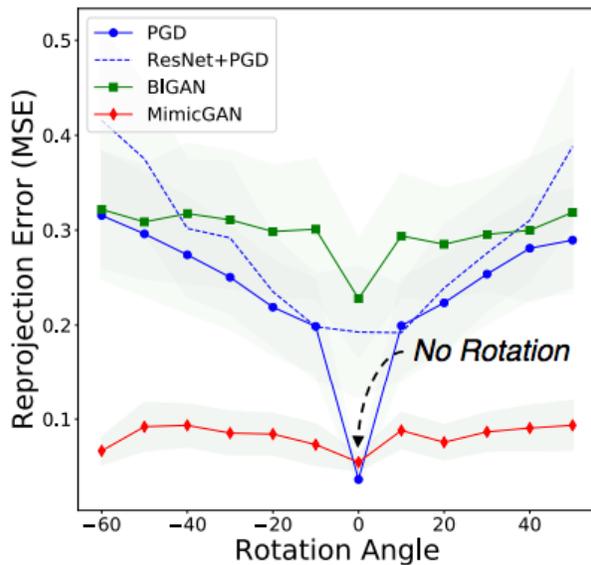
$$z^*, \hat{f}^* = \arg \min_{z \in \mathbb{R}^d} \|\mathcal{F}^?(Y) - \hat{f}(\mathcal{G}(z))\|$$

Final projection is given by

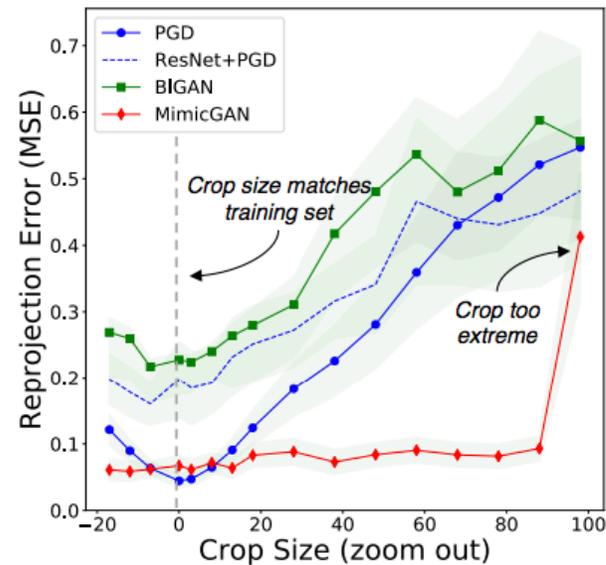
$$\mathcal{G}(z^*)$$

A shallow neural network is  
“trained” to estimate the corruption

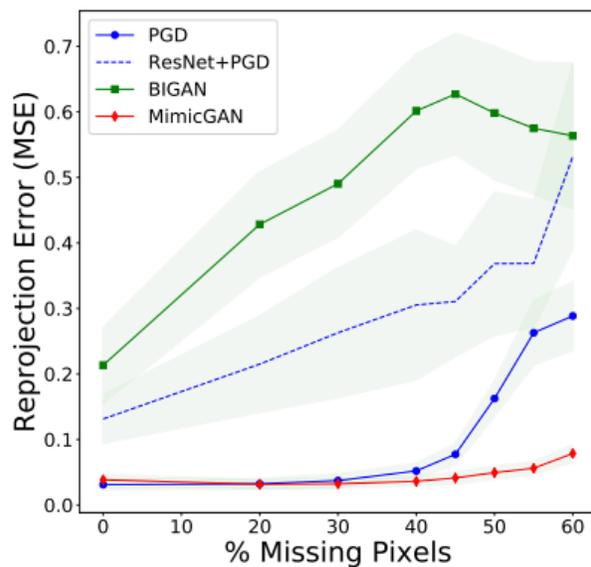
# Robustness Experiments



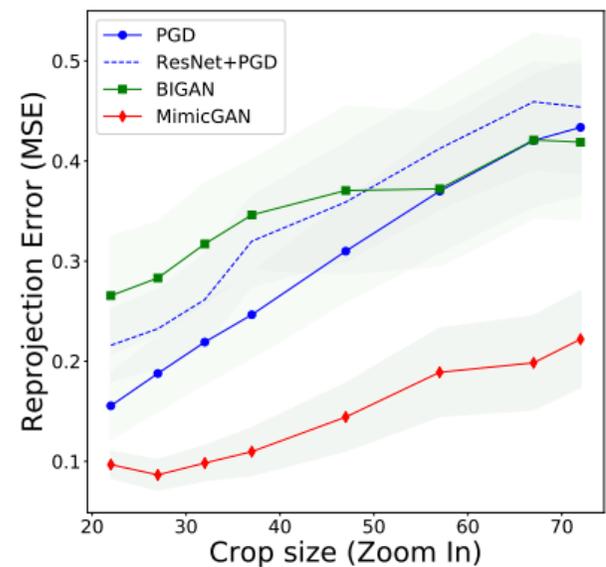
(a) Robustness to rotations



(b) Robustness to scale



(c) Projections under missing pixels



(d) Projections under missing context

Observed



MimicGAN  
(proposed)



PGD





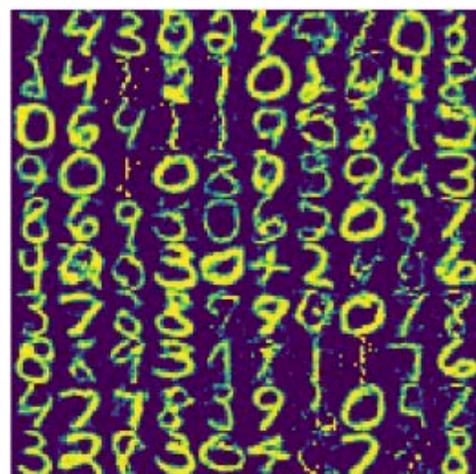
Projected onto MNIST manifold with MimicGAN



USPS Target



Projected onto MNIST manifold with PGD



Projected onto USPS manifold with MimicGAN



MNIST Target



Projected onto USPS manifold with PGD

(b) MNIST→USPS



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