

Generalized Multiple Importance Sampling for Source Characterization in Multi-epoch Imaging

CASIS Workshop

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Michael D. Schneider
Physics Division

In collaboration with:
William Dawson (LLNL)
Joshua Meyers (Stanford)

The Large Synoptic Survey Telescope (LSST)

Construction start: 2014

First light: 2020

Survey end: 2030

8.4m telescope

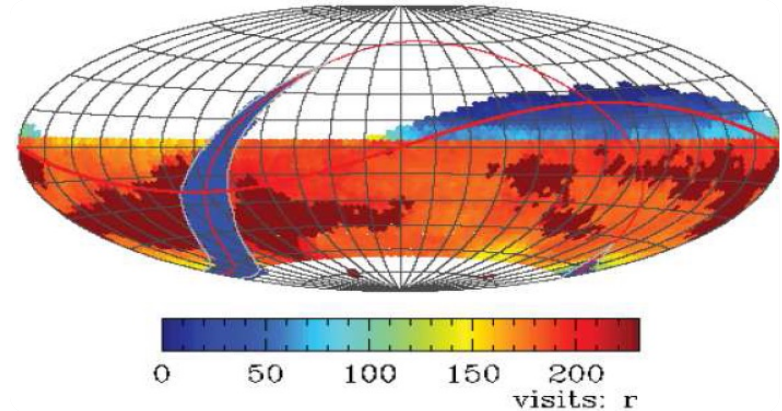
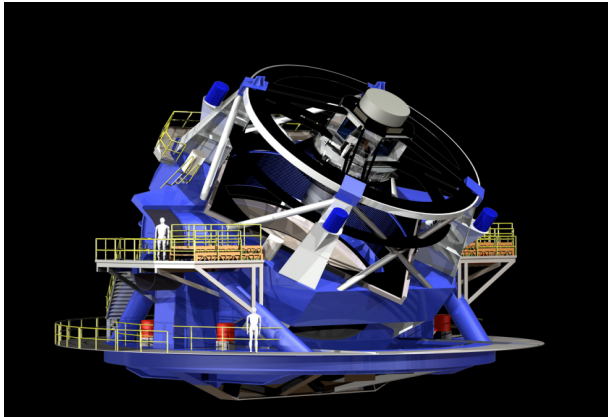
18,000+ deg²

10 maarcsec astrometry

r<24.5 (<27.5@10yr)

6 broad optical bands

0.5-1% photometry



3.2Gpix camera

2x15sec exp/2sec read

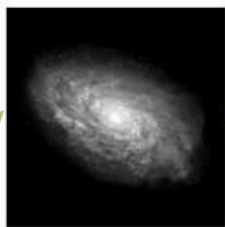
15TB/night

20 B objects

Imaging the visible sky, once every 3 days, for 10 years (**825 revisits**)

Science use case: Weak gravitational lensing of galaxies

Galaxies: Intrinsic galaxy shapes to measured image:

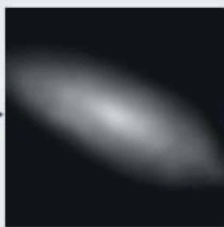


Intrinsic galaxy
(shape unknown)

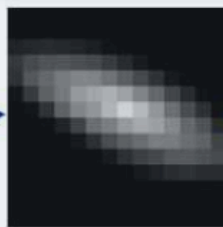


Gravitational lensing
causes a *shear* (*g*)

Want this



Atmosphere and telescope
cause a convolution



Detectors measure
a pixelated image

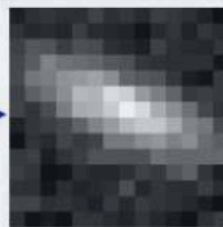
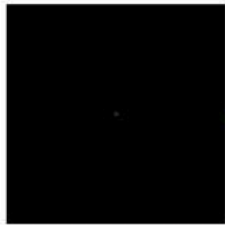


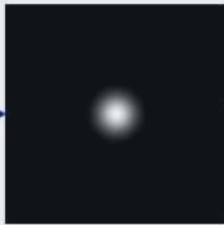
Image also
contains noise

Marginalize

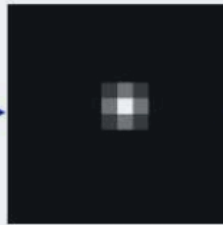
Stars: Point sources to star images:



Intrinsic star
(point source)



Atmosphere and telescope
cause a convolution



Detectors measure
a pixelated image

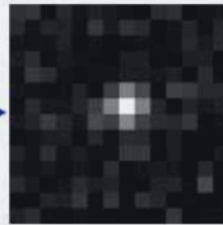


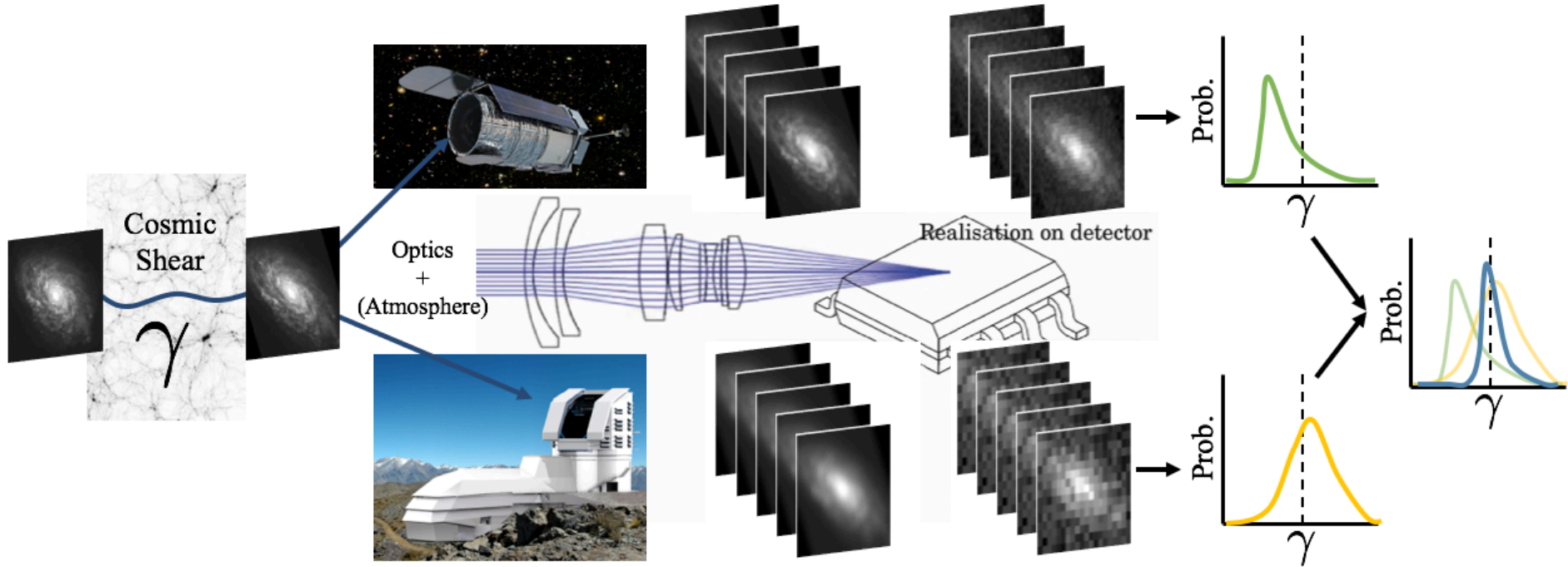
Image also
contains noise

Constrained by

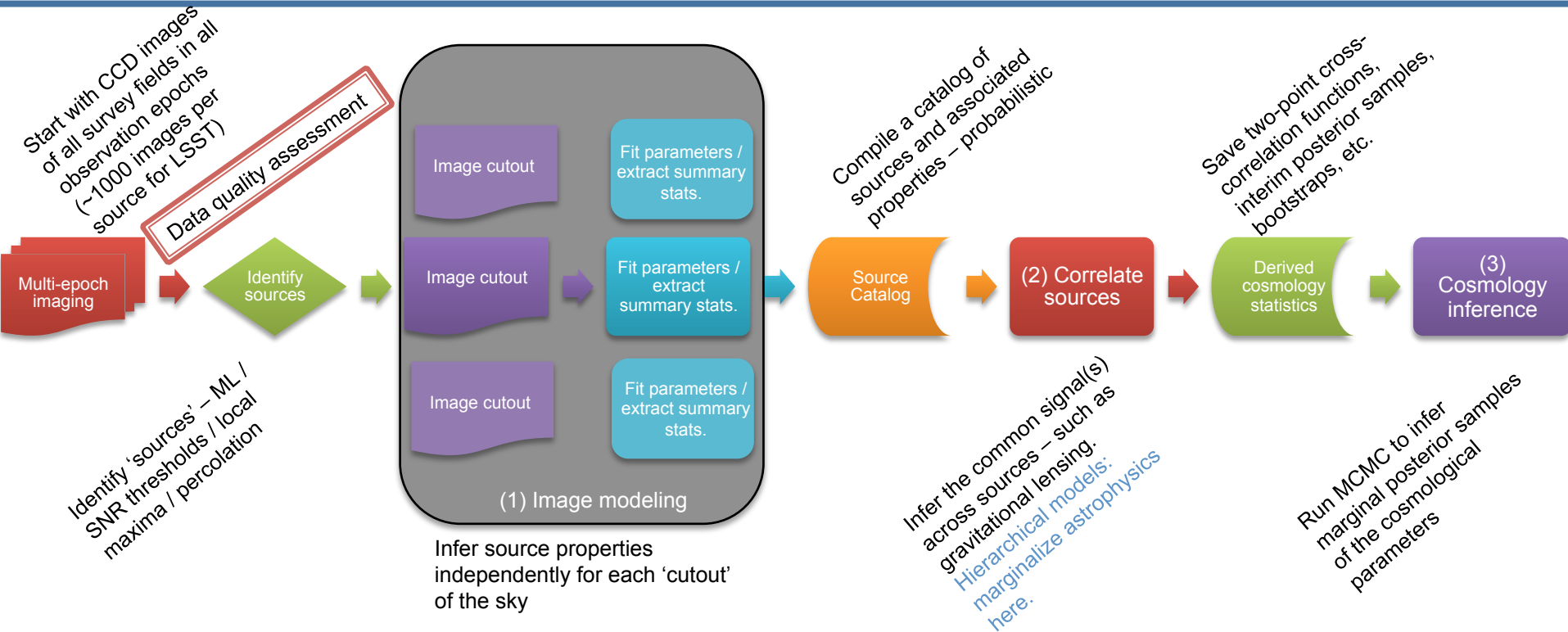
Unknown &
dominates
signal

Unlike in the past, we will have many observations of the same sources that must be combined, while marginalizing distinct systematic errors

– A new processing paradigm

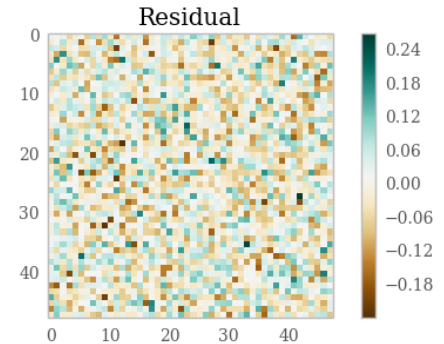
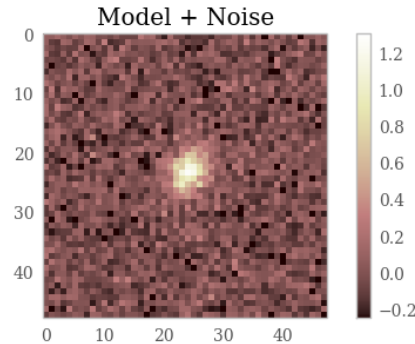
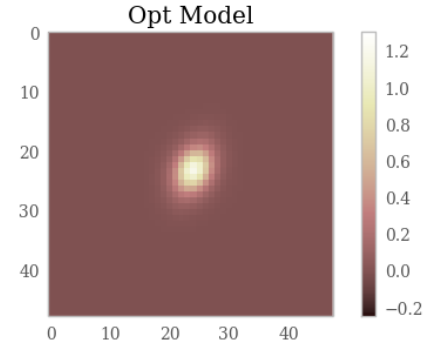
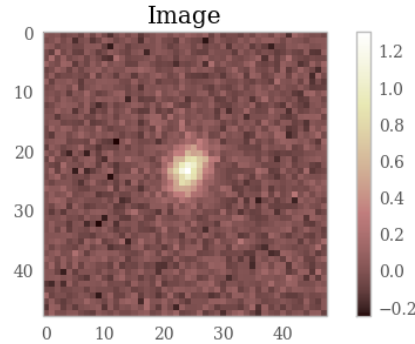
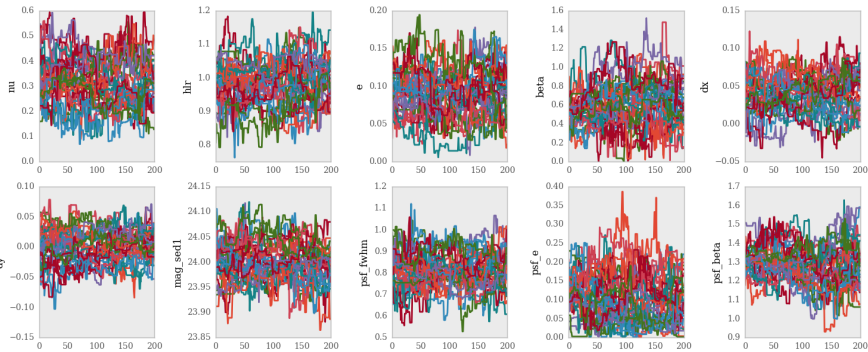


The data management & analysis pipeline components for gravitational weak lensing and galaxy clustering with LSST



Source characterization via probabilistic image modeling

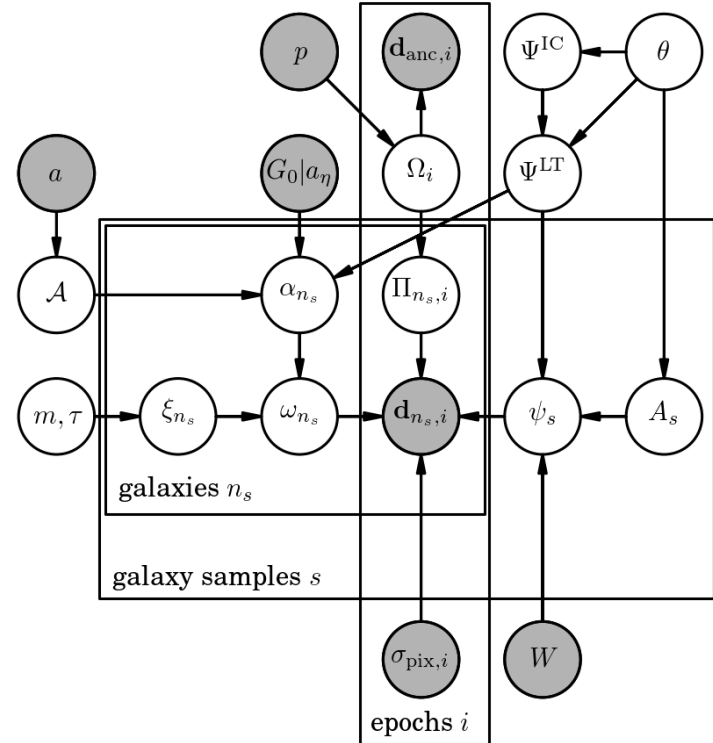
Infer image model parameters via MCMC, then marginalize as part of a hierarchical model for the distributions of galaxy and systematics parameters



The complete statistical model for cosmic shear

arXiv:1411.2608

Parameter	Description
θ	Cosmological parameters
Ψ^{IC}	Initial conditions for the 3D gravitational potential
Ψ^{LT}	Late-time 3D gravitational potential
ψ_s	2D lens potential (given source photo- z bin s)
A_s	Parameters for the line-of-sight source distribution
$\Pi_{n_s,i}$	PSF for galaxy n_s observed in epoch i
Ω_i	Observing conditions in epoch i
$\{\omega_{n_s}\}$	Galaxy model parameters; $n_s = 1, \dots, n_{\text{gal},s}$
$\{\alpha_{n_s}\}$	Parameters for the distribution of $\{\omega_{n_s}\}$
$\{\xi_{n_s}\}$	Scaling parameters for $\{\omega_{n_s}\}$
m, τ	Hyperprior parameters for $\{\xi_{n_s}\}$
\mathcal{A}	Hyperparameter for $\{\alpha_{n_s}\}$ classifications
$\{\mathbf{d}_{n_s,i}\}$	Pixel data for galaxies $n_s = 1, \dots, n_{\text{gal},s}$ in epoch i
$G_0 a_\eta$	Prior specification for $\{\alpha_{n_s}\}$
s	Source sample (e.g., photo- z bin)
W	Survey window function
$\mathbf{d}_{\text{anc},i}$	Ancillary data for PSF in epoch i
p	Prior params. for observing conditions
a	Prior params. for \mathcal{A}
$\sigma_{\text{pix},i}$	Pixel noise r.m.s. in epoch i
I	Model selection assumptions



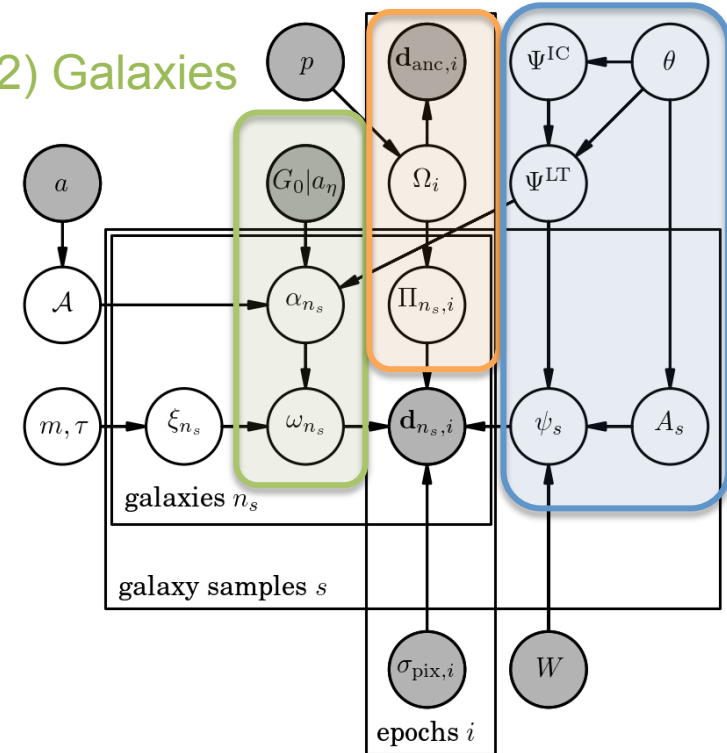
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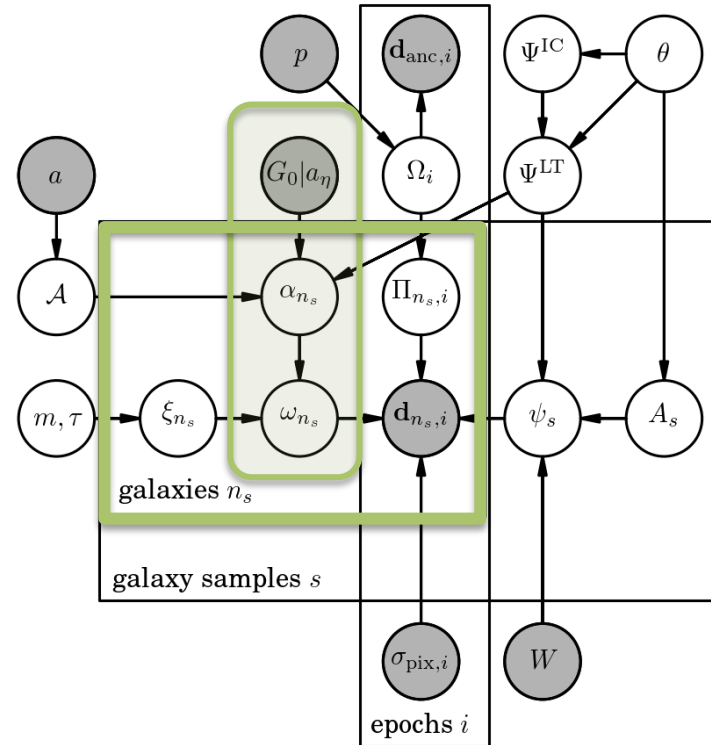
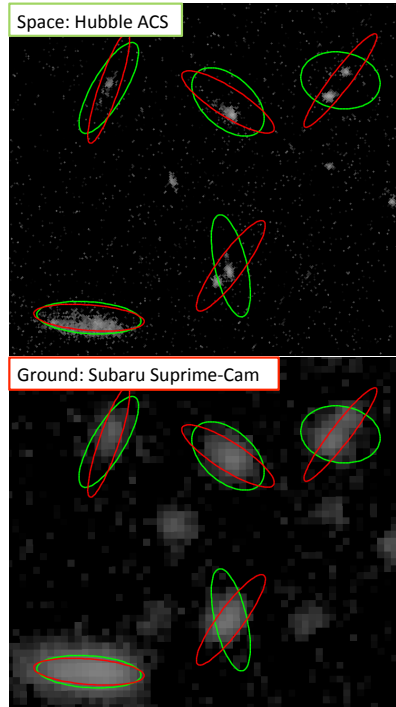
1) PSFs 3) Cosmology

2) Galaxies



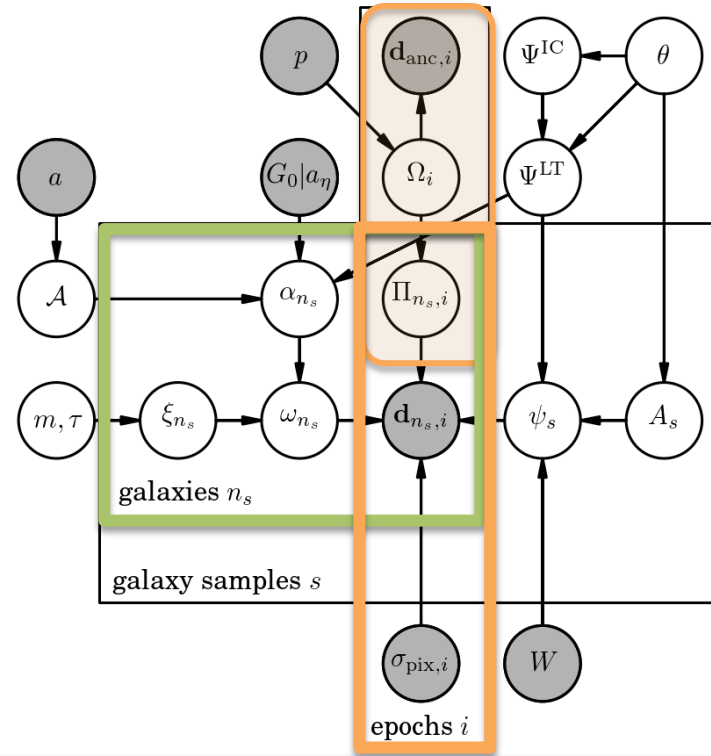
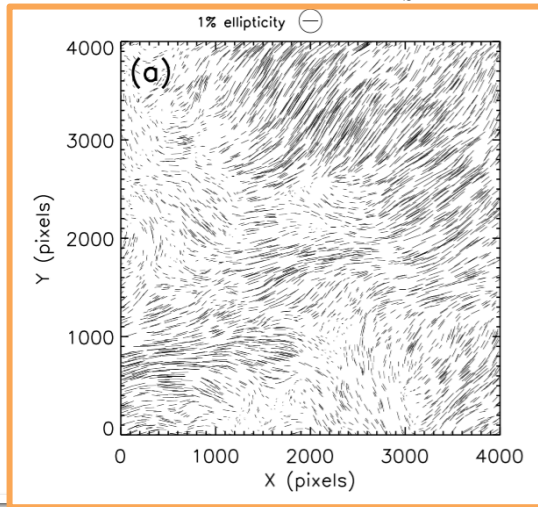
Naïve approach is intractable

- Galaxy models be joint fitted to all available epochs i



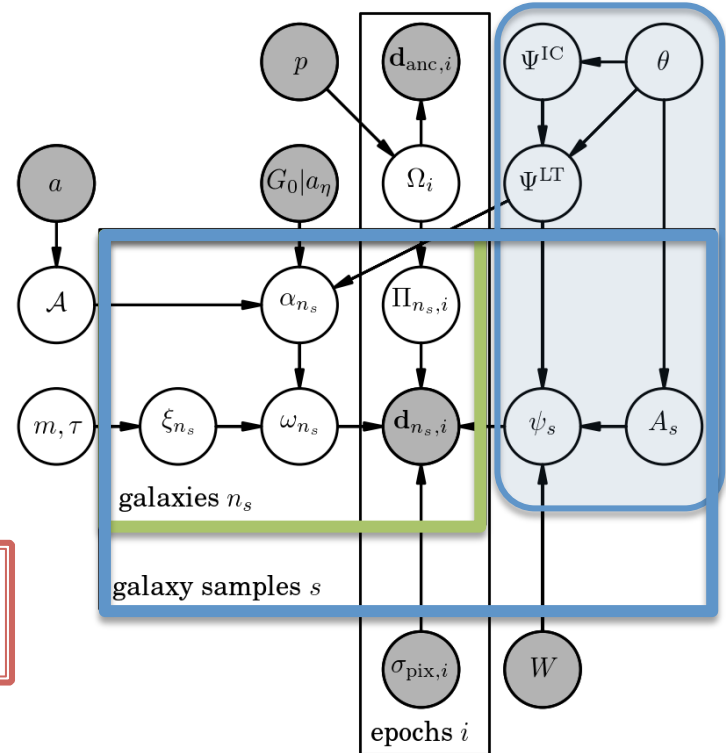
Naïve approach is intractable

- Galaxy models be joint fitted to all available epochs i
- PSF models** must be joint fitted to all galaxies in an exposure n_s



Naïve approach is intractable

1. Galaxy models be joint fitted to all available epochs i
2. PSF models must be joint fitted to all galaxies in an exposure n_s
3. **Cosmology** must be joint fitted to all galaxy samples & epochs



The principled inference requires fitting all pixels of all surveys simultaneously

Importance sampling to separate the sampling of individual galaxies: **The pseudo-marginal likelihood**

Want:

$$\Pr(\mathbf{d}|\alpha) \propto \prod_{n=1}^{n_{\text{gal}}} \int d\omega_n \underbrace{\Pr(\omega_n|\alpha)}_{\text{Galaxy dist.}} \underbrace{\Pr(\mathbf{d}_{n,i}|\omega_n)}_{\text{Likelihood}}$$

Have samples from:

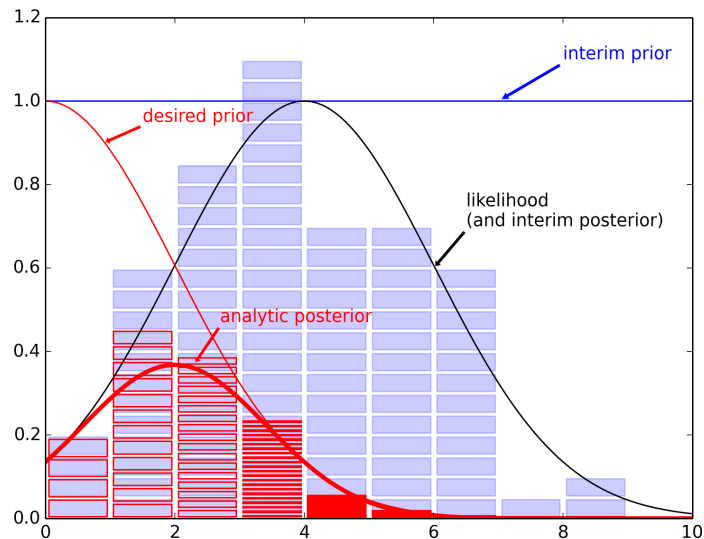
$$\Pr(\omega_n|\mathbf{d}_n, I_0)$$

'Interim prior' specification

Importance sampling:

$$\Pr(\mathbf{d}_n|\alpha) \approx \frac{Z_n}{K} \sum_k \frac{\Pr(\omega_{nk}|\alpha)}{\Pr(\omega_{nk}|I_0)},$$

$$\Pr(\mathbf{d}|\alpha) = \prod_{n=1}^{n_{\text{gal}}} \Pr(\mathbf{d}_n|\alpha).$$



Credit: J. Meyers

How do we combine multiple observations of the same galaxy?

Naïvely we must joint fit all epochs simultaneously

Problem: Imagine we have fit pixel data from LSST year 1.
How do we incorporate year 2 observations without redoing (expensive) calculations?

$$\Pr(\mathbf{d}_n | \alpha, \{\Pi_i\}) = \int d\omega_n \Pr(\omega_n | \alpha) \prod_{i=1}^{n_{\text{epochs}}} \Pr(\mathbf{d}_{n,i} | \omega_n, \Pi_i)$$

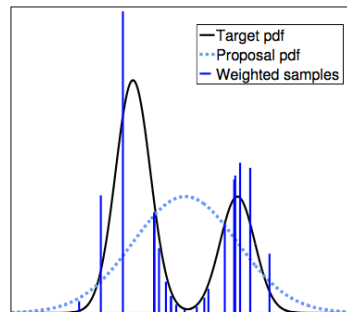
Solution: Consider single-epoch samples as draws from a multi-modal importance sampling distribution:

$$q(\omega_n) = \frac{1}{n_{\text{epochs}}} \sum_{i=1}^{n_{\text{epochs}}} \Pr(\omega_n | \mathbf{d}_{n,i}, \Pi_i, I_0)$$

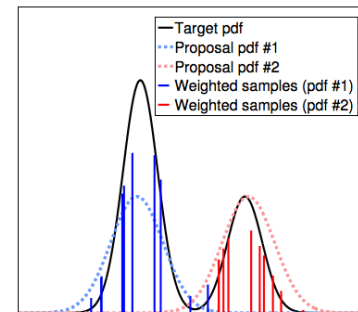
arXiv:1511.03095

Generalized Multiple Importance Sampling

Elvira, Martino, Luengo, & Bugallo



(a) Single proposal pdf (standard IS).



(b) Two proposal pdfs (MIS).

Fig. 1: Approximation of the target pdf, $\pi(\mathbf{x})$, by the random measure χ .

Generalized multiple importance sampling (MIS) weights

MIS sampling distribution: sample from the conditional posterior for each epoch individually

$$q(\omega_n) = \frac{1}{n_{\text{epochs}}} \sum_{i=1}^{n_{\text{epochs}}} \Pr(\omega_n | \mathbf{d}_{n,i}, \Pi_i, I_0)$$

MIS weights: Evaluate the ratio of the conditional posterior for each epoch i to that of the MIS sampling distribution

$$w_i = \frac{\Pr(\mathbf{d}_{n,i} | \omega_n, \Pi_i) \Pr(\omega_n | \alpha)}{\sum_{i=1}^{n_{\text{epochs}}} \Pr(\mathbf{d}_{n,i} | \omega_n, \Pi_i) \Pr(\omega_n | I_0)}$$

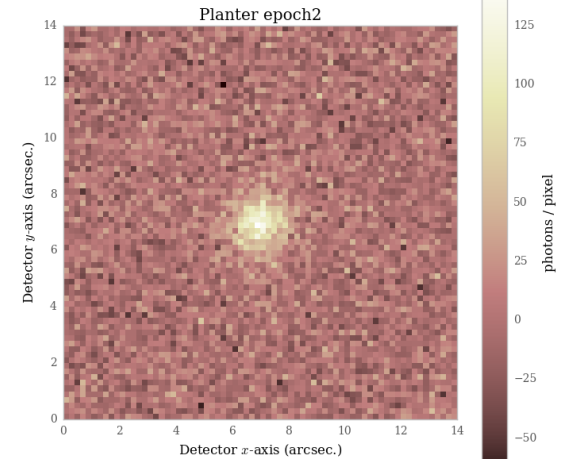
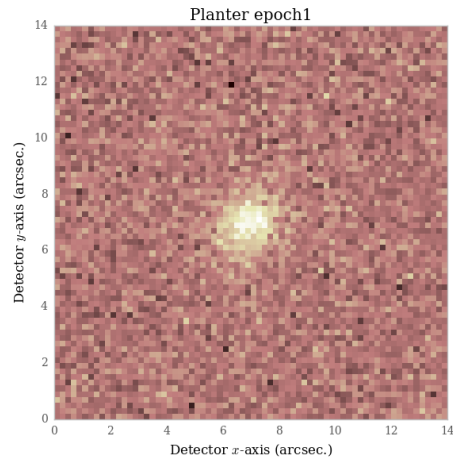
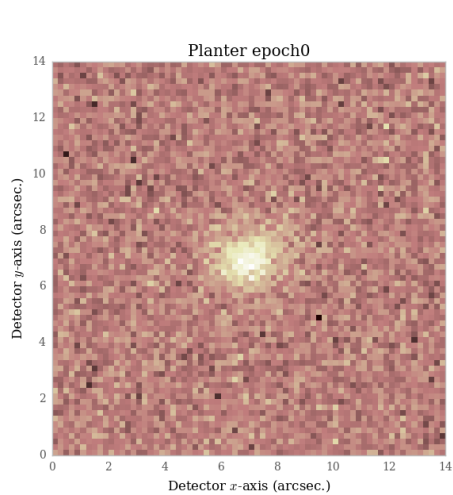
'cross-pollination' needed:

Evaluate the likelihood of epoch i given model parameter samples from epoch j , for all combinations of i, j .

A standard scatter / gather operation

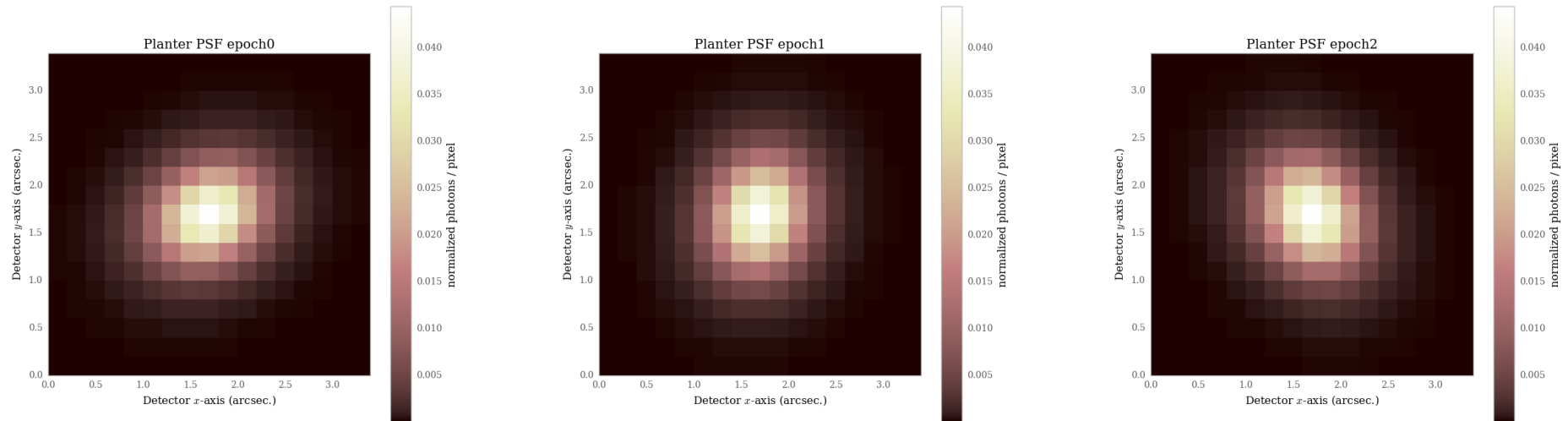
$$\Pr(\mathbf{d}_{n,i} | \omega_n^{(j)}, \Pi_i)$$

Example: 1 galaxy, 3 epochs – fit the galaxy model parameters



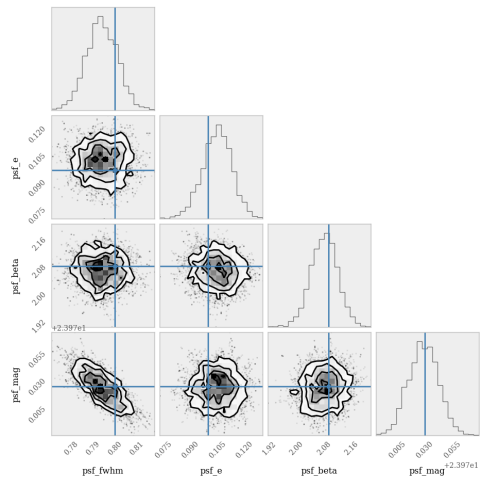
Each epoch has highly elliptical PSFs ($|e| = 0.1$) of same size, but different orientations

The PSF FWHM also matches the galaxy HLR making the single-epoch inferences noticeably different from each other. There is therefore a large gain of information in combining epochs.

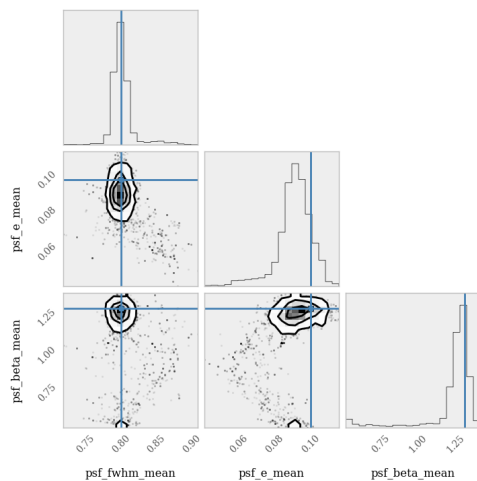


Interim posterior samples at each stage of the PSF hierarchical model

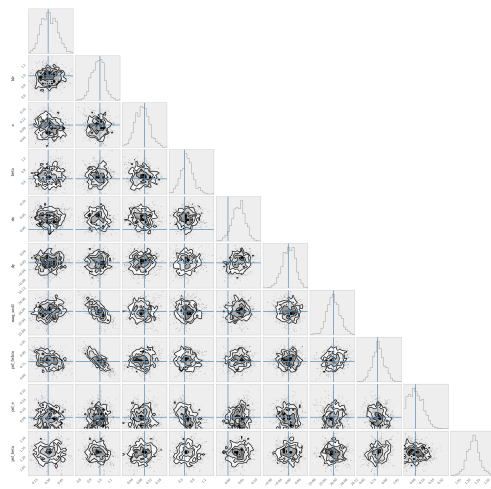
1) Fit stars



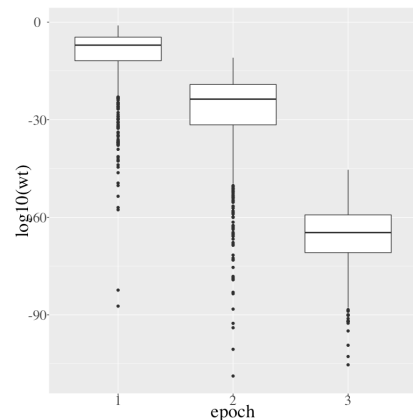
2) Constrain PSF model



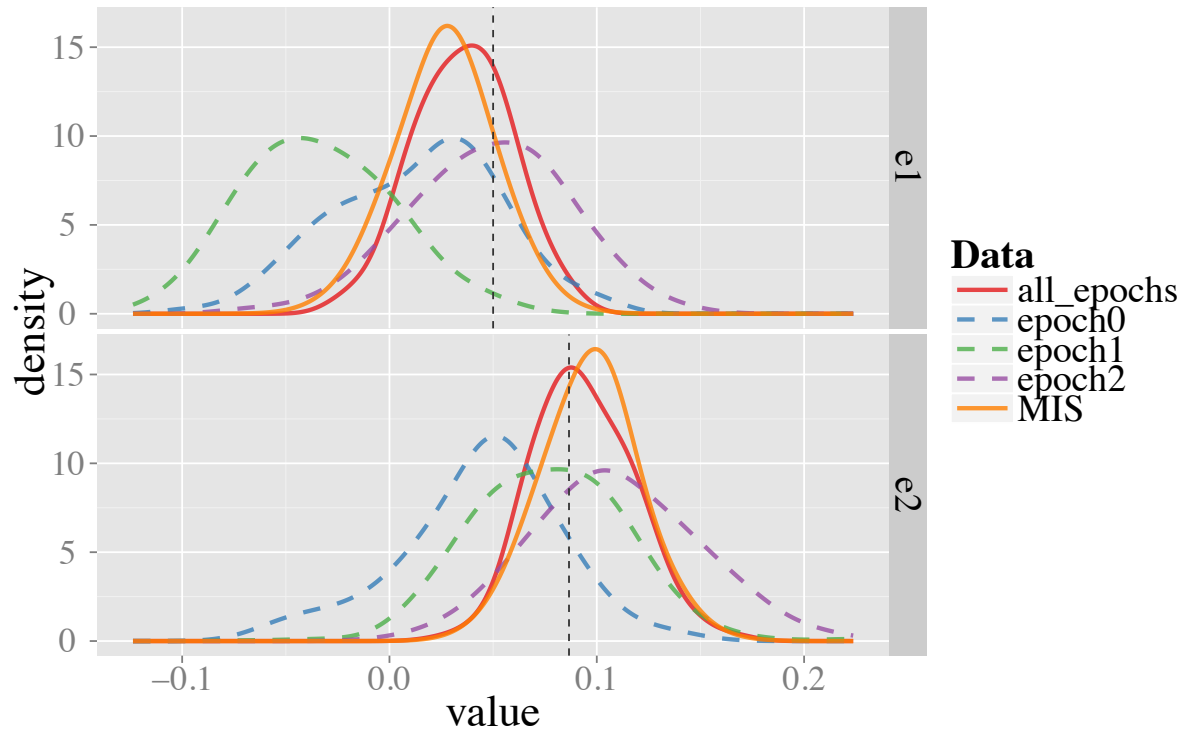
3) Fit galaxies & PSFs



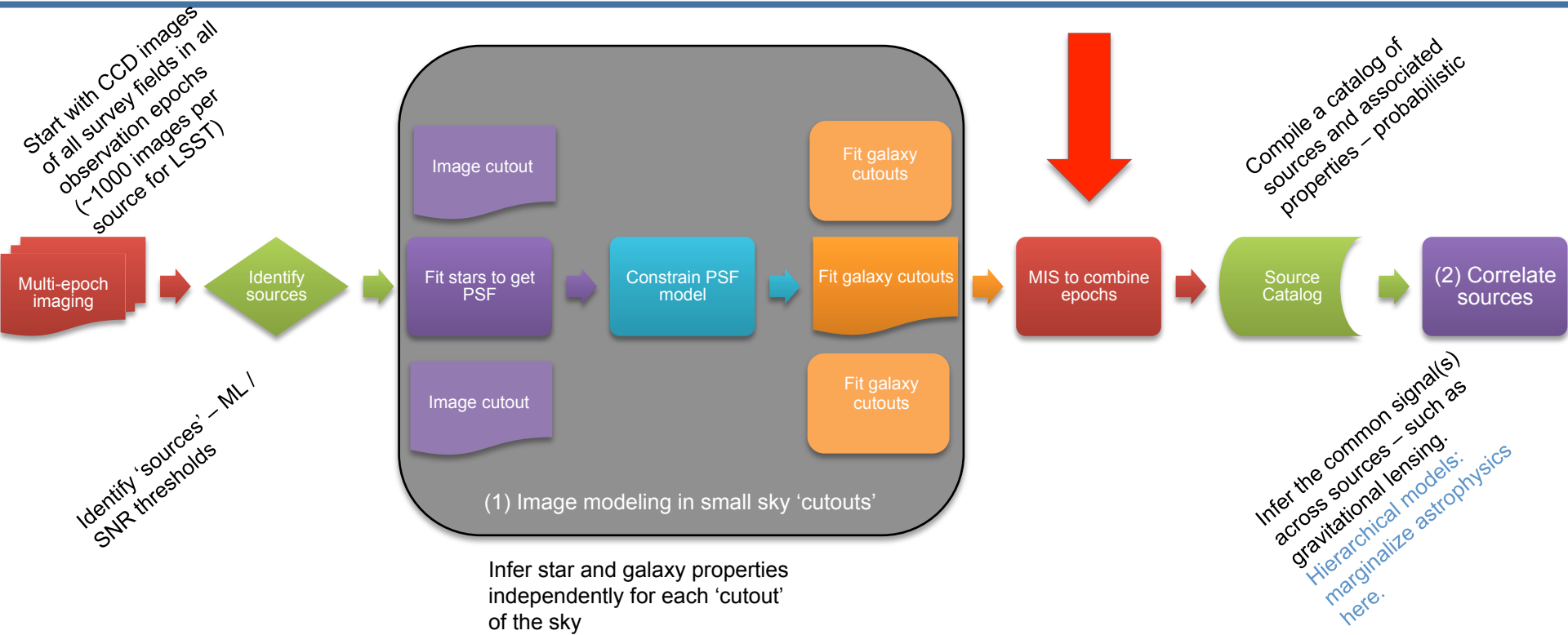
4) Calculate MIS weights to combine epochs



Comparison of single-epoch and combined epochs marginal posteriors



Data management and analysis pipeline: MIS-enabled



Conclusions

- Cosmic shear is systematics limited & signal is dominated by PSF and astrophysics
 - A probabilistic approach is warranted to infer a small signal and mitigate biases
- Importance sampling methods allow tractable approaches to a probabilistic forward model of LSST imaging
 - With billions of galaxies and hundreds of epochs per galaxy modeling LSST imaging requires an approach to separating analyses of data subsets, even though statistically correlated
- We are able to sample from a probabilistic model with multiple hierarchies to marginalize both correlated image systematics and astrophysical properties of galaxies



Outline

- The science: cosmic shear in LSST
- Probabilistic pipeline introduction
- The problem of multiple epochs and MIS solution
- MIS example
- Pipeline redux in light of MIS
- Conclusions

Marginalizing PSFs: MIS makes this tractable

- LSST will have ~ 200 epochs per object per filter
 - We aim to marginalize the PSF $\prod_{n,i}$ in every epoch
 - The marginalization is constrained by:
 - Consistency of PSF realizations over the focal plane for each epoch
 - Consistency of the underlying source model across epochs
- Simplest approach (statistically, not computationally): Infer galaxy models given all epoch imaging simultaneously
 - “Interim” samples are of size: ~ 10 galaxy params + $200 * \sim 4$ PSF params = $\sim 1k$ parameters!

