

# **Time Resolved Measurement of Transient Acoustic Waves using A Frequency Domain Photoacoustic Microscopy System**

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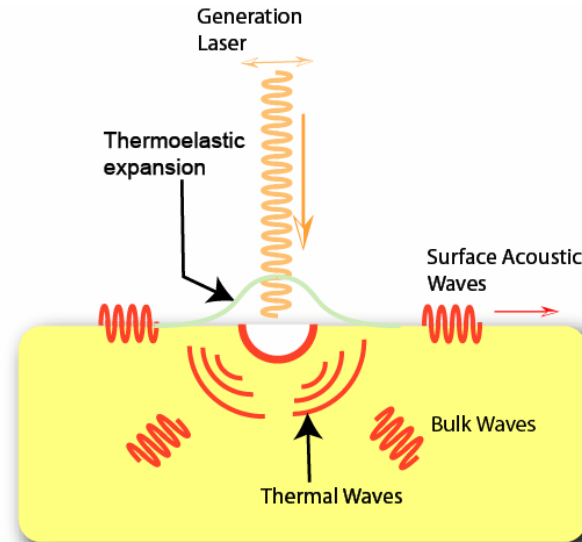
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## OUTLINE

- Photoacoustic Microscopy: Background and Applications
- Motivation - Signal to Noise Ratio Considerations
- Experimental Setup
- Time Domain Signal Analysis
- Conclusions

# PHOTOACOUSTIC MICROSCOPY (Laser Based Ultrasonics)



- Pulsed or modulated CW laser illuminates the sample surface
- Absorption of incident light leads to local heating of the sample
- Thermoelastic expansion of the heat active region generates coherent acoustic waves
- Generated acoustic waves are detected by measuring the sample surface displacement or elastic strain using optical detection systems

## **Advantages of Photoacoustic Microscopy over Conventional Acoustic Microscopy**

- Non-contact, remote materials inspection
- Extremely high fidelity (generation and detection of acoustic waves over GHz bandwidth possible)
- High spatial resolution (important for the characterization of MEMS and nanoscale structures)
- Rapid scanning possible leading to reduced inspection time

### **Applications Include the Measurement of:**

- Dimensional properties such as thickness or density of thin films and membranes
  - Mechanical properties such as residual stress, elastic modulus, Poisson's ratio
  - Micro- structural properties such as grain-size and texture
  - Surface properties, surface defects, coating quality
-

## Laser Sources used for Acoustic Wave Generation

### **GENERATION OF BROADBAND ACOUSTIC WAVES**

- **Nanosecond sources: Q- switched lasers**
- **Femtosecond and picosecond sources: Mode-locked lasers**

### **GENERATION OF NARROWBAND ACOUSTIC WAVES**

- **Temporally modulated pulsed laser sources: Mode-locked or Q switched pulse trains, AO modulated Q switched lasers, Laser array Sources**

### **OTHER:**

- **Direct modulated CW laser: Generated with Pseudo-random Sequence**

(Pierce *et. al.*, Appl. Phys. Lett. 72(9), 1030, 1997, Madaras and Anastasi, AIP (509) 303, 2000 )

## Signal to Noise Ratio (SNR) of an Optical Detection System

**Noise Sources: Thermal noise, shot noise, intensity and wavelength instabilities, etc** (Wagner and Spicer, *J. Opt. Sc. Am B* 4(8), 1316, 1997, Wagner, *Physical Acoustics*)

**Shot Noise Limited SNR:**  $SNR \propto \delta \sqrt{\frac{P}{B}}$

$\delta$  = Acoustic wave amplitude

$P$  = Optical power incident on the photodetector

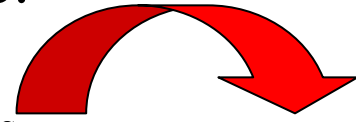
$B$  = Bandwidth of the detection system

Approach Used to Improve the SNR: Focus the acoustic energy into an extremely narrow frequency band and match the bandwidth of the detection system to the acoustic spectrum.

## Towards the Development of a Photoacoustic Microscopy System with an Improved Signal to Noise Ratio (SNR)

High resolution Measurements Require:

- tightly focused excitation source
- generation of high frequency acoustic waves



Pulsed Lasers Can be Used **BUT**:

- energy must be kept low:  $\delta \downarrow$
- acoustic energy distributed over a large bandwidth:  $B \uparrow$

NET RESULT

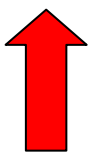
$$SNR \propto \delta \sqrt{\frac{P}{B}}$$



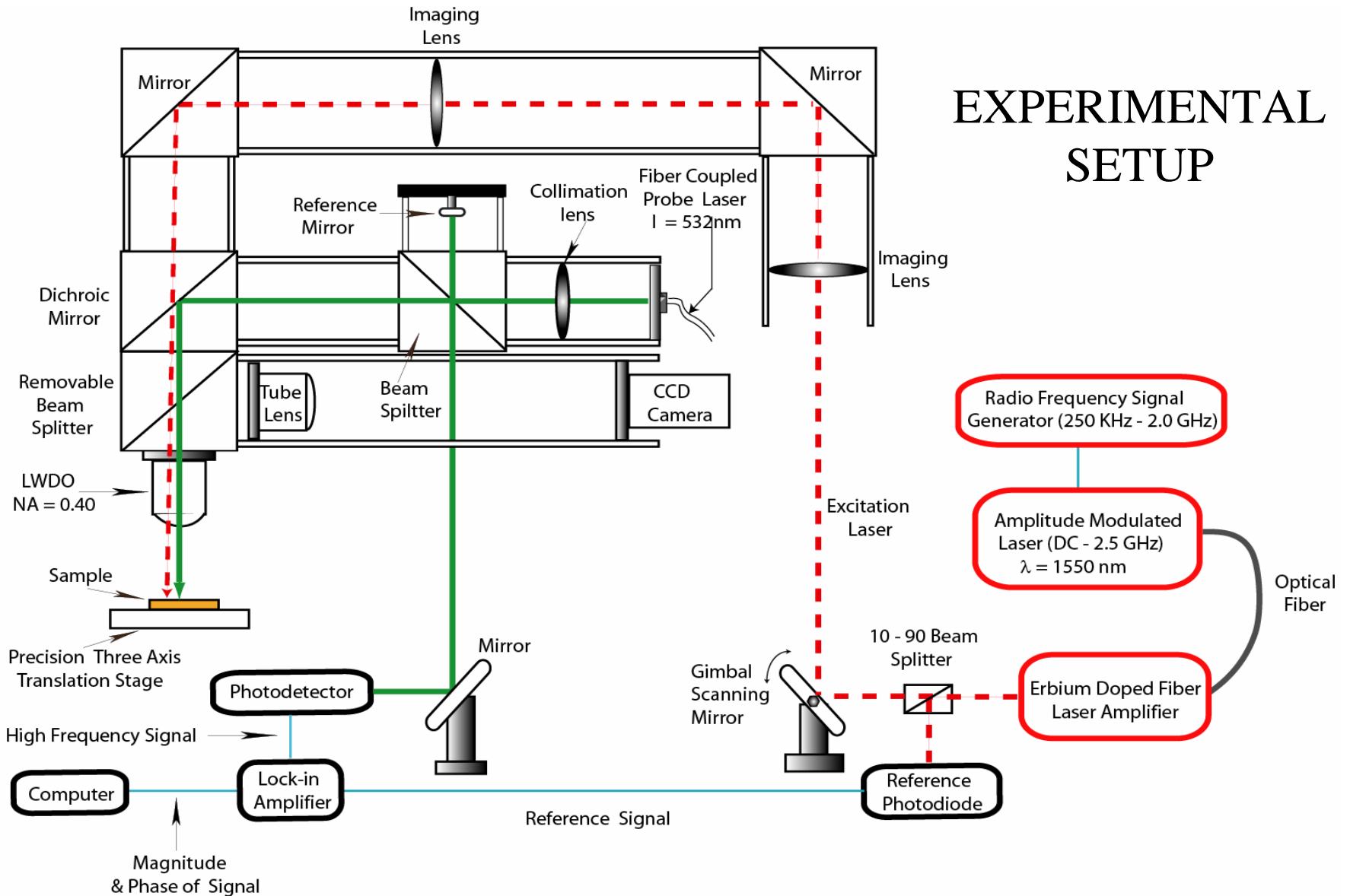
Our Approach: Low power, sinusoidally modulated CW laser source

- power low:  $\delta \downarrow$
- acoustic energy focused into extremely narrow frequency band:  $B \downarrow \downarrow \downarrow$

NET RESULT  $SNR \propto \delta \sqrt{\frac{P}{B}}$

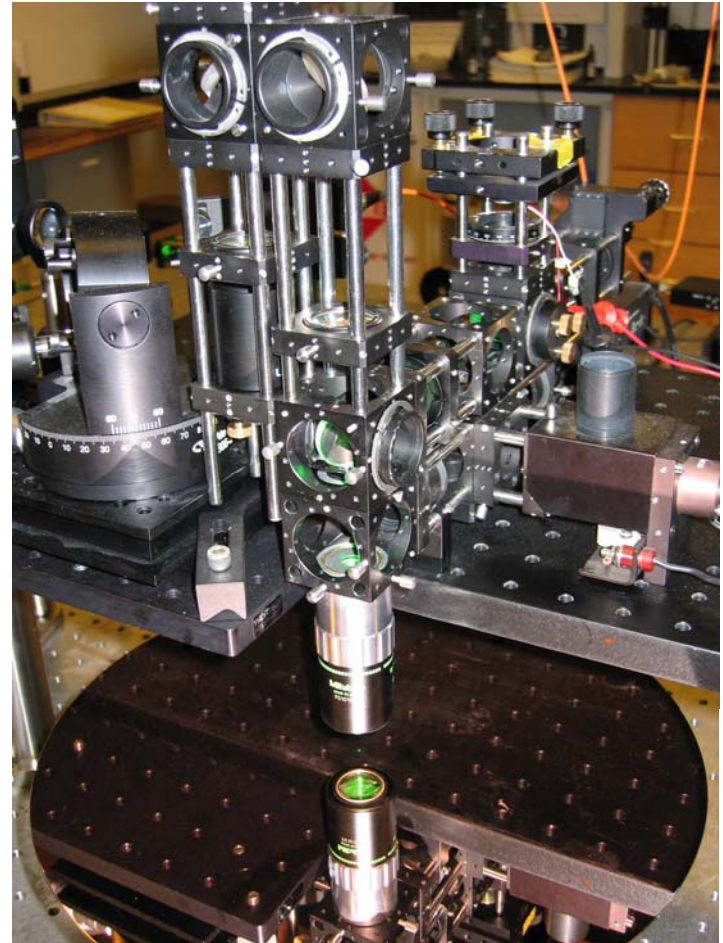
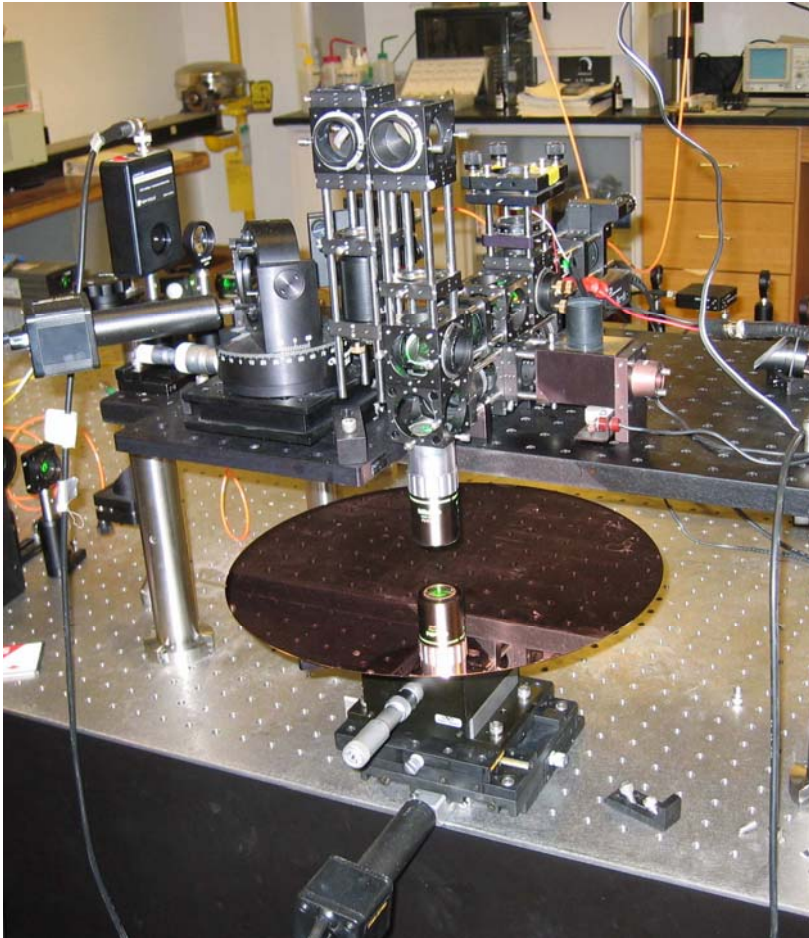


# EXPERIMENTAL SETUP





## EXPERIMENTAL SETUP



## **CHALLENGE: EXTRACT QUANTITATIVE INFORMATION**

- Measured magnitude and phase of the signal at  $f$  are influenced by the entire acoustic field
- Extraction of materials properties/ quantitative NDE difficult

## **TIME DOMAIN RECONSTRUCTION**

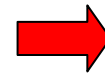
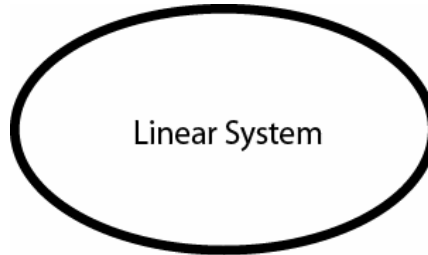
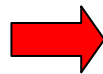
- Material is excited using sinusoidal modulation at given frequency ( $f$ ) and at a fixed source to receiver distance
- Magnitude and phase of the signal at  $f$  is recorded
- Measurement is repeated over the frequency range of interest
- A time domain “pulsed” response is constructed

**FREQUENCY DOMAIN**

$$f_1(t) = I_1(f_1) \cos(2\pi f_1 t)$$

$$\vdots$$

$$f_N(t) = I_N(f_N) \cos(2\pi f_N t)$$



$$u_1(t) = A(f_1) \cos(2\pi f_1 t + \varphi(f_1))$$

$$\vdots$$

$$u_N(t) = A(f_N) \cos(2\pi f_N t + \varphi(f_N))$$

**SUM  
(INPUT)**



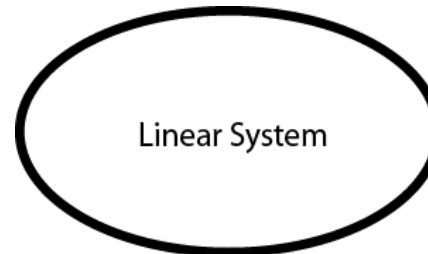
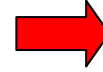
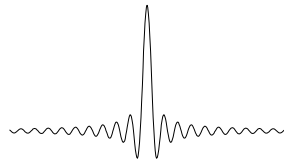
$$i(t) = \frac{1}{N} \sum_{n=1}^N I_n(nf_0) \cos(2\pi nf_0 t)$$

**SUM  
(OUTPUT)**



$$S(t) = \frac{1}{N} \sum_{n=1}^N A_n(nf_0) \cos[2\pi nf_0 t + \varphi(nf_0)]$$

**TIME DOMAIN**



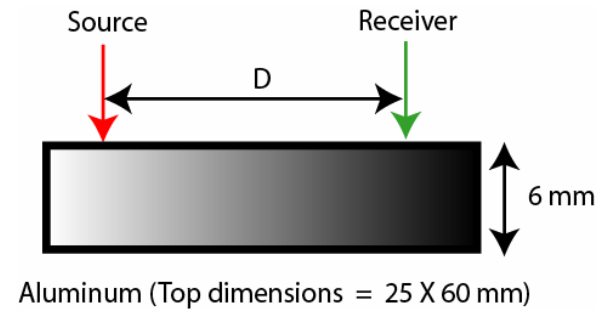
**INPUT "PULSE"**

**OUTPUT SIGNAL**

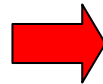
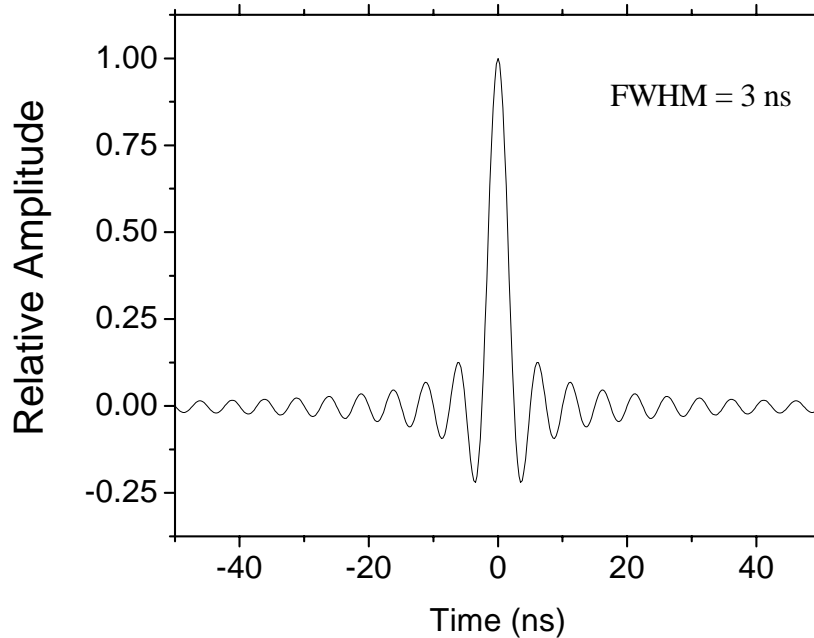
## TIME DOMAIN RECONSTRUCTION

Frequency range = 1 – 200 MHz

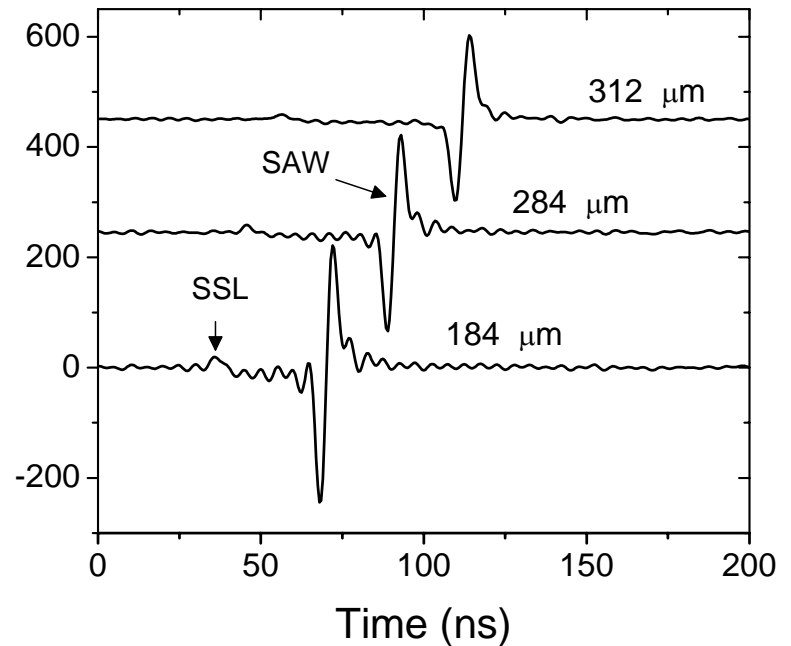
$$f_0 = 1.0 \text{ MHz}$$



### SYNTHESIZED INPUT ‘PULSE’



### SYNTHESIZED RESPONSE



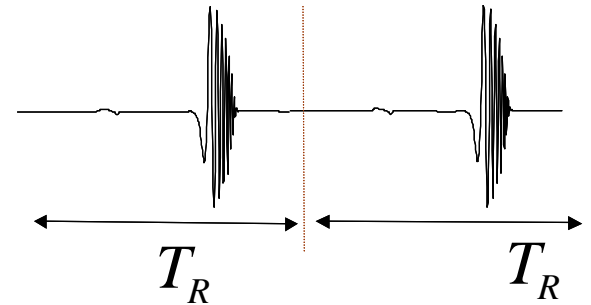
## Choice of Frequency Resolution $f_0$

### TIME DOMAIN ALIASING

❑ Reconstructed time window repeats after  $T_R = \frac{1}{f_0}$

❑ Arrivals after  $T_R$  will appear as “alias arrivals” at  $T < T_R$

❑  $f_0$  must be chosen such that  $T_R$  is greater than the decay time ( $\tau$ ) of the acoustic field to unambiguously reconstruct the time domain response.



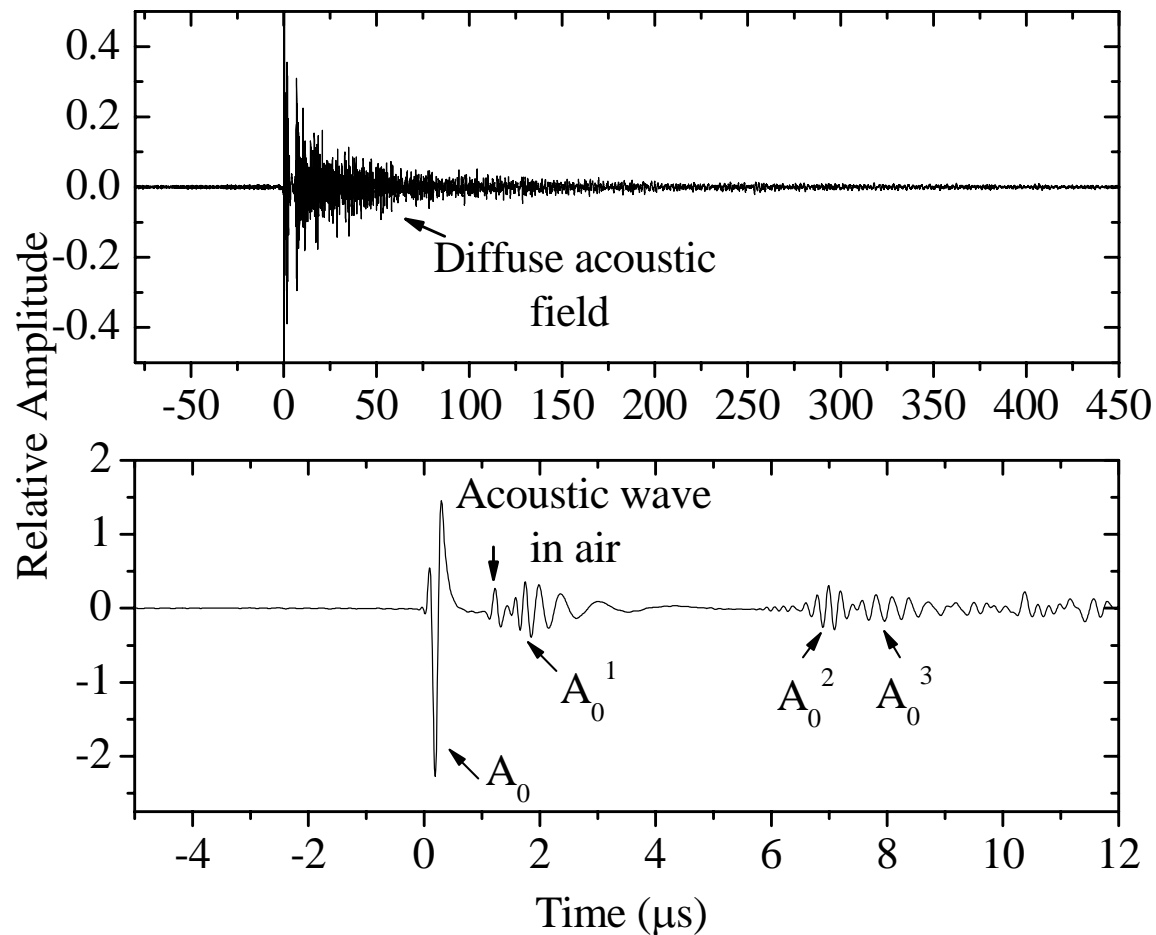
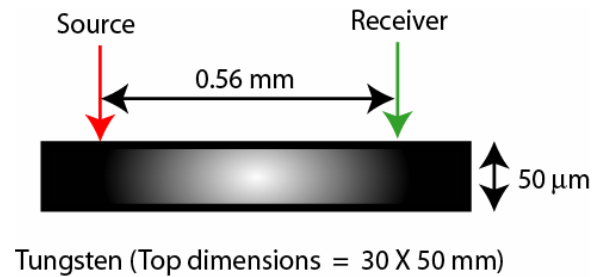
### SIGNAL TO NOISE RATIO (SNR)

❑ SNR improves with number of frequency samples acquired ( $N$ )  $SNR \propto N^{\frac{1}{2}}$

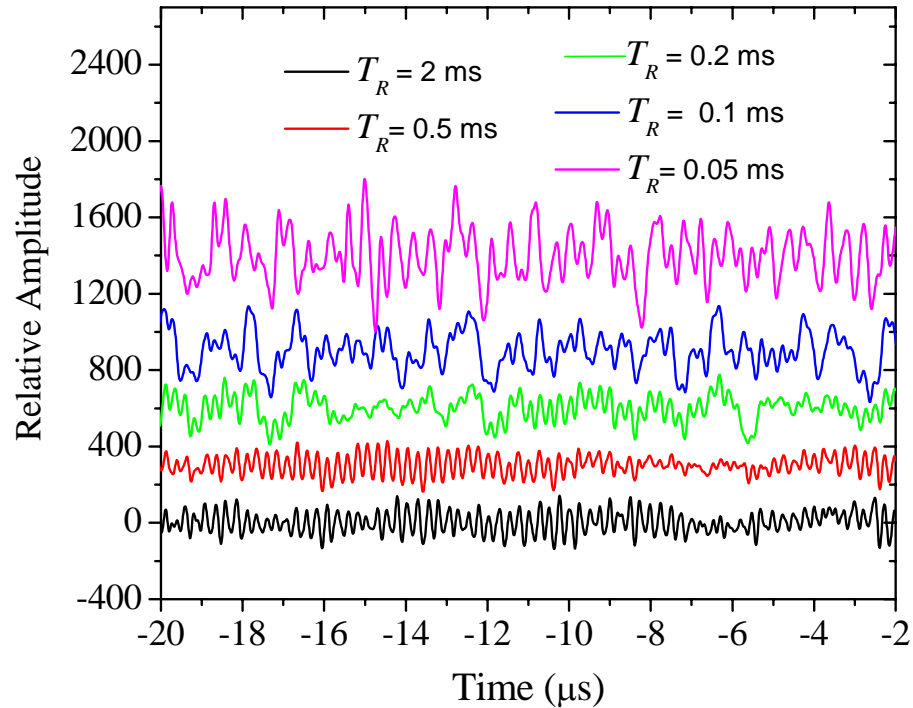
❑  $\tau$  allows for selection of minimum  $f_0$ , oversampling is analogous to averaging in the time domain

## TIME DOMAIN ALIASING

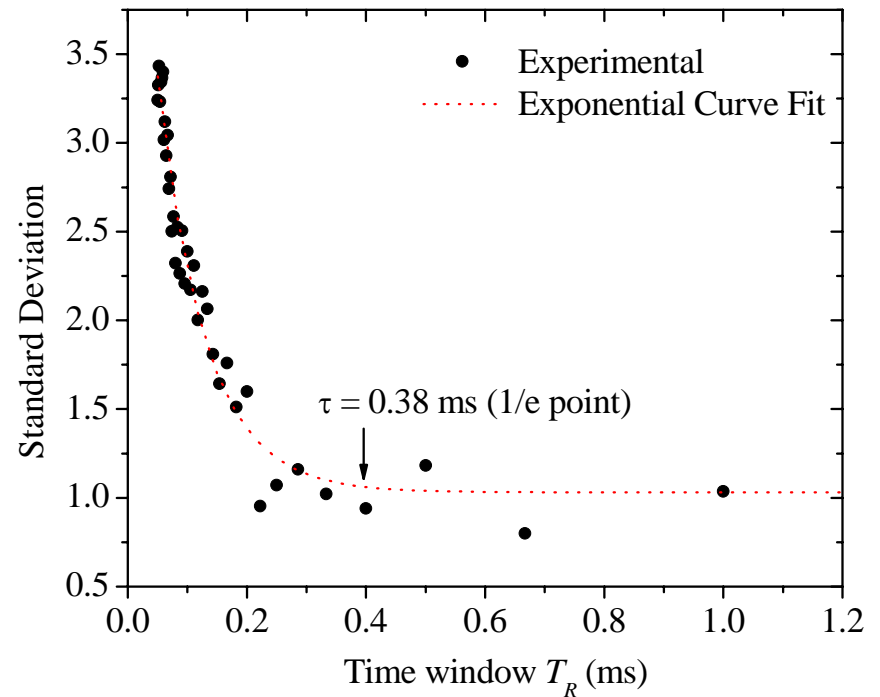
Frequency range = 0.2 – 10 MHz,  $f_0 = 0.5$  KHz,  $T_R = 2$  ms



## NOISE IN SYNTHESIZED WAVEFORMS



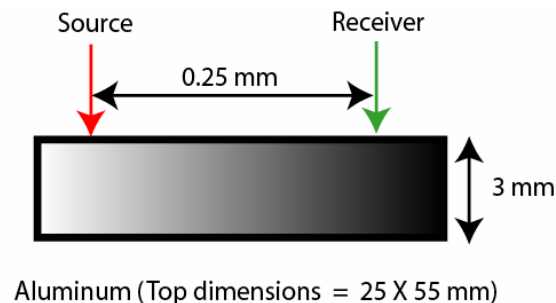
## NOISE AS A FUNCTION OF TIME WINDOW



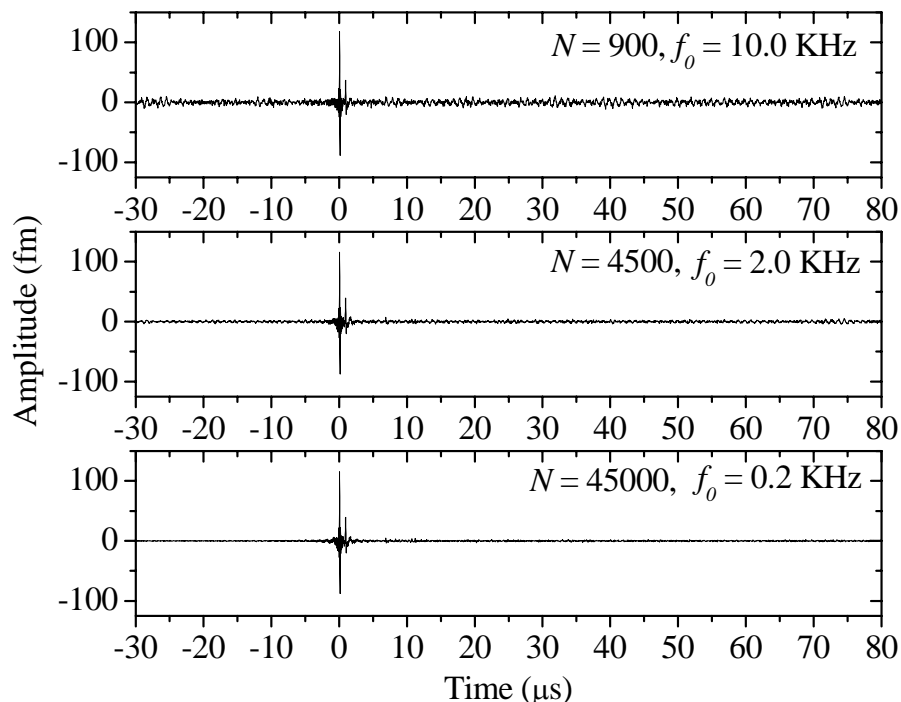
## SIGNAL TO NOISE RATIO (SNR)

- Here the acoustic decay time is  $< 20\mu\text{s}$
- SNR dependence on  $N$  confirmed

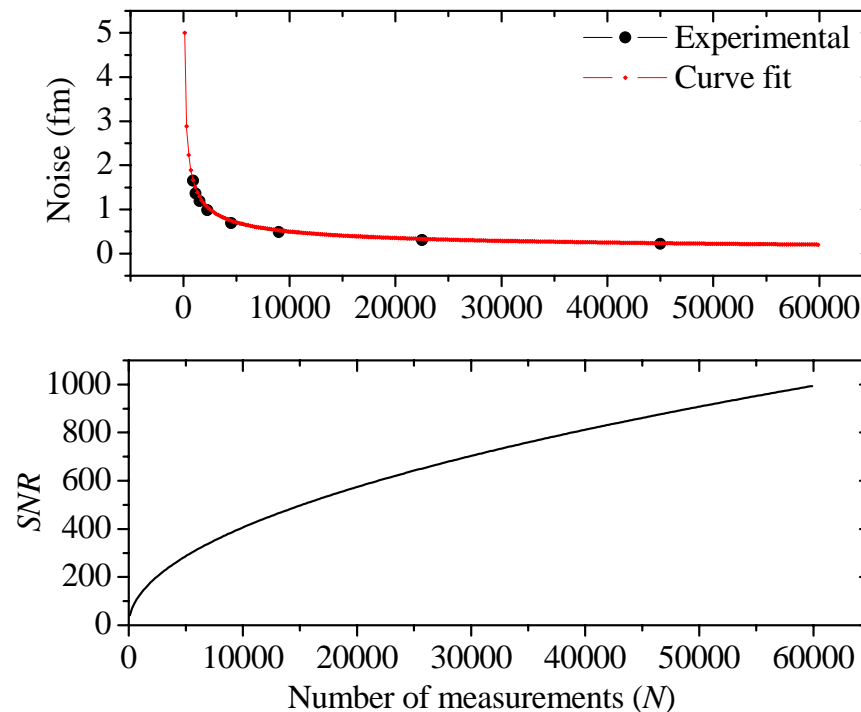
Frequency range = 1 – 10 MHz



## SYNTHESIZED WAVEFORMS

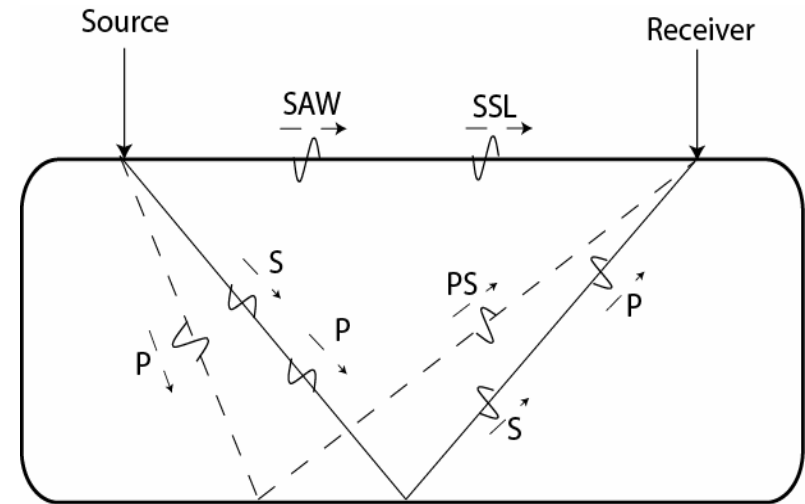
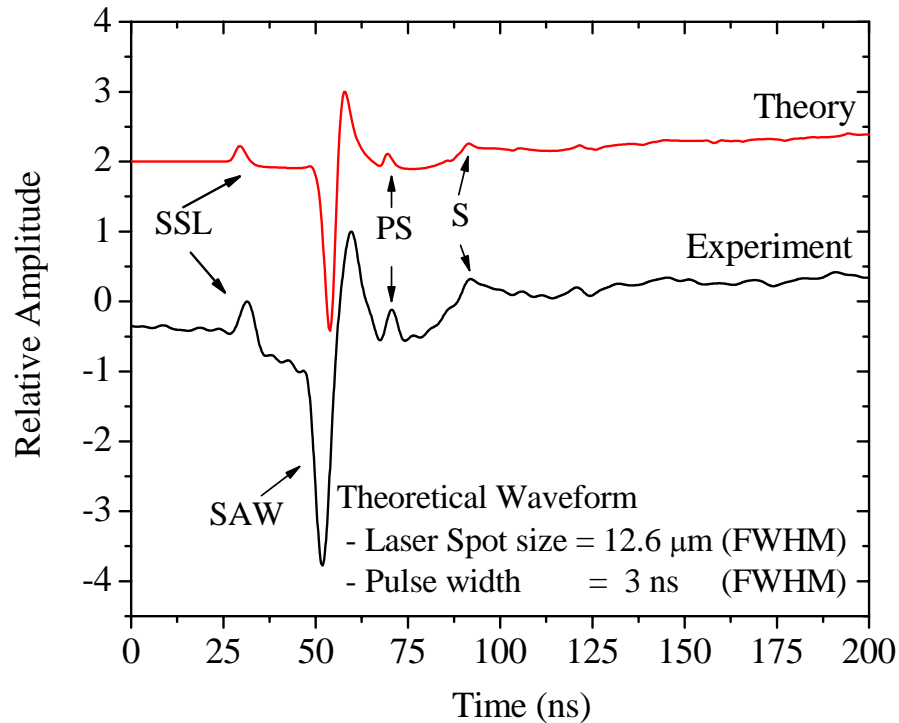


## SNR

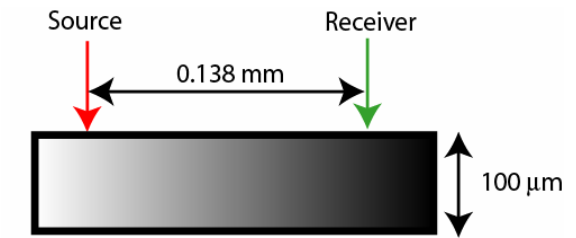




# High Frequency Measurements: Theory and Experiment



Frequency range = 1 –200 MHz  
 $f_0 = 10.0 \text{ KHz}$ ,  $T_0 = 0.1 \text{ ms}$



Tungsten (Top dimensions = 40 X 50 mm)

## CONCLUSIONS

- ❑ A frequency domain photoacoustic microscopy system was developed for the characterization of micro- and nanoscale materials.
- ❑ The displacement sensitivity of the optical detection system was shown to be in the femtometer range for a detection bandwidth of 1 Hz.
- ❑ Temporal resolution of transient acoustic waves was obtained by synthesizing a pulse response from the frequency domain data