



**Progress towards an electro-acoustic resonance technique for determining
quantitative material and geometrical properties in high contrast
multi-layer elastic structures.**

UCRL-PRES-208104

Karl Fisher

*New Technologies Engineering Division
Lawrence Livermore National Laboratory*

*This work was performed under the auspices of the U.S. Department of Energy by University of California,
Lawrence Livermore National Laboratory under Contract W-7405-Eng-48.*

K. Fisher LLNL CASIS '04

Overview



- **Background**
- **Development**
- **Experimental**
- **Current Results**

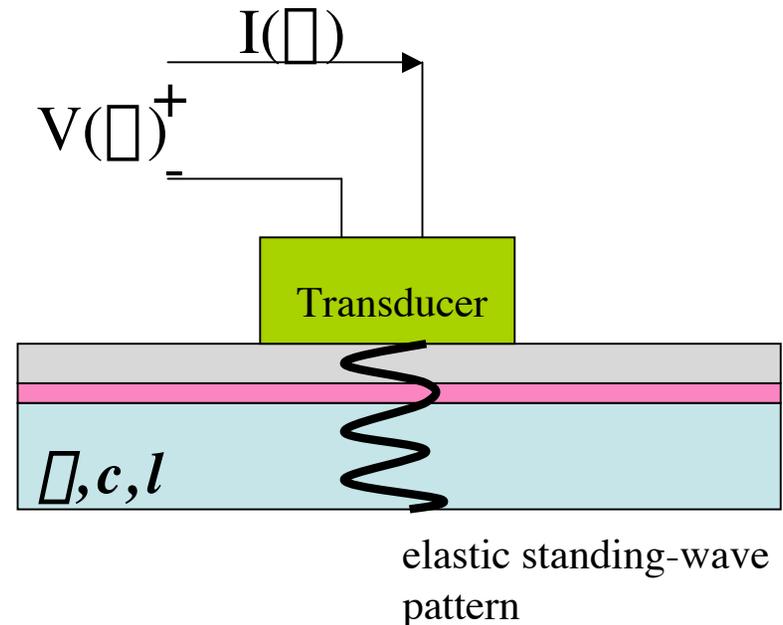
Background



Basic Concept: By driving the Transducer at a sinusoidal voltage, $V(\omega)$ an elastic standing wave pattern, (mechanical mode) is created in each layer. The current, $I(\omega)$ into the transducer can be simultaneously measured. The resulting *ratio* is the total electrical impedance, $Z_{TOTAL}(\omega)$ of the entire system.

$$Z_{TOTAL}(\omega) = \frac{V(\omega)}{I(\omega)}$$

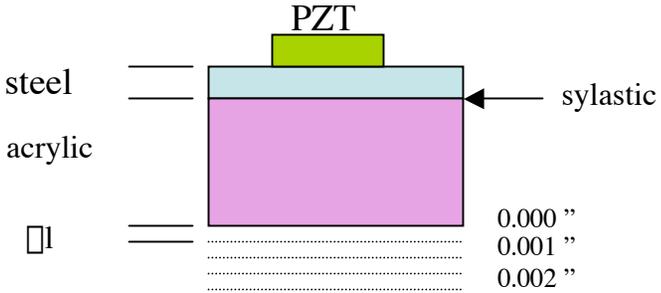
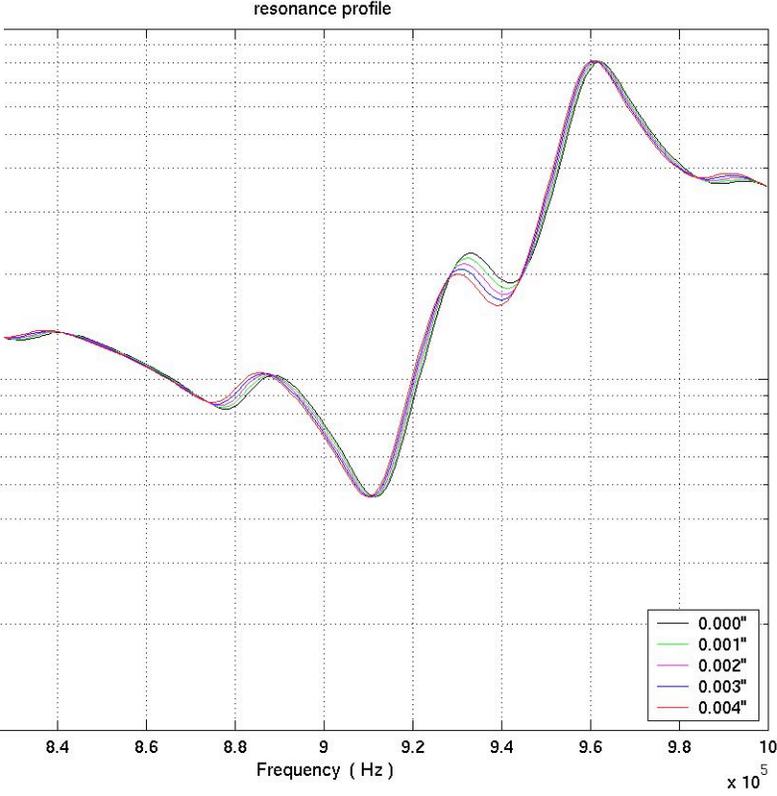
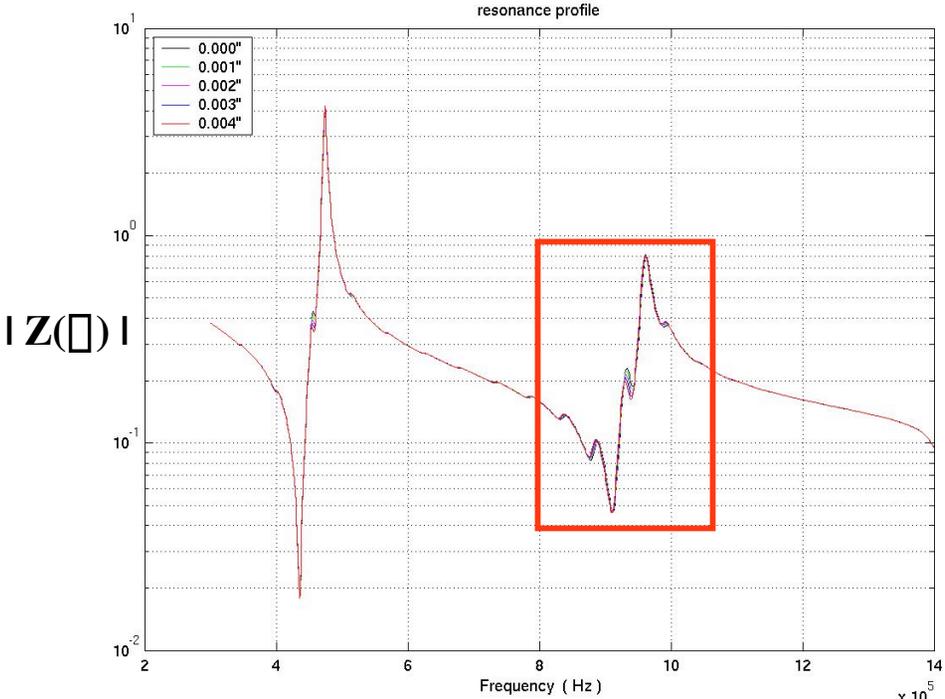
$$Z_{TOTAL}(\omega) = \underbrace{\frac{1}{\omega C_o}}_{\text{“electrical”}} + f_n \underbrace{\tan\left(\frac{\omega}{c_n} l_n\right)}_{\text{“mechanical”}}$$



- At a **mechanical resonance**

$$\frac{\omega}{c_n} l_n = \omega(2m+1) \quad I(\omega_0) \longrightarrow 0, \text{ and } Z_{TOTAL}(\omega_0) \longrightarrow \text{‘BIG’}$$

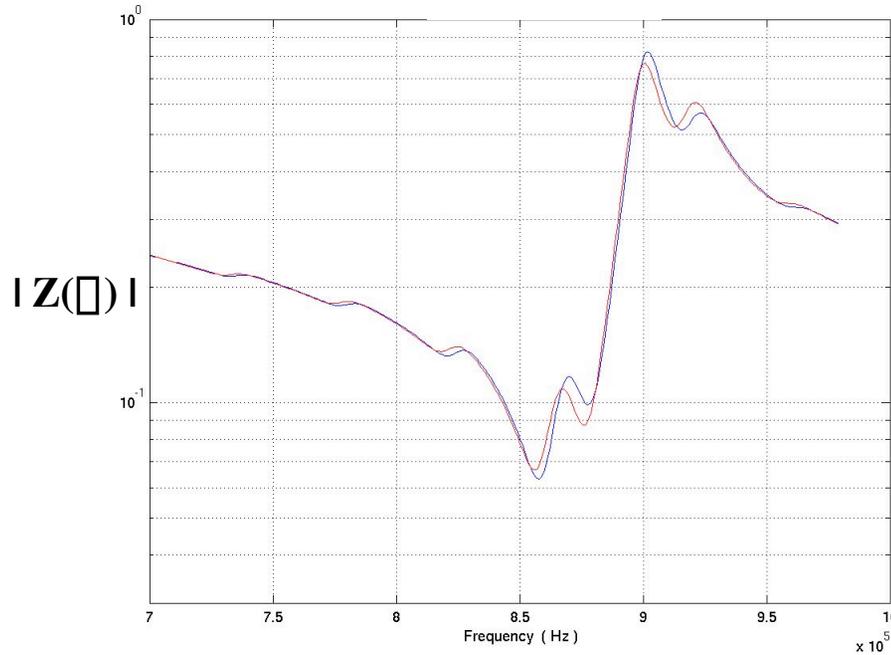
Impedance sizing study



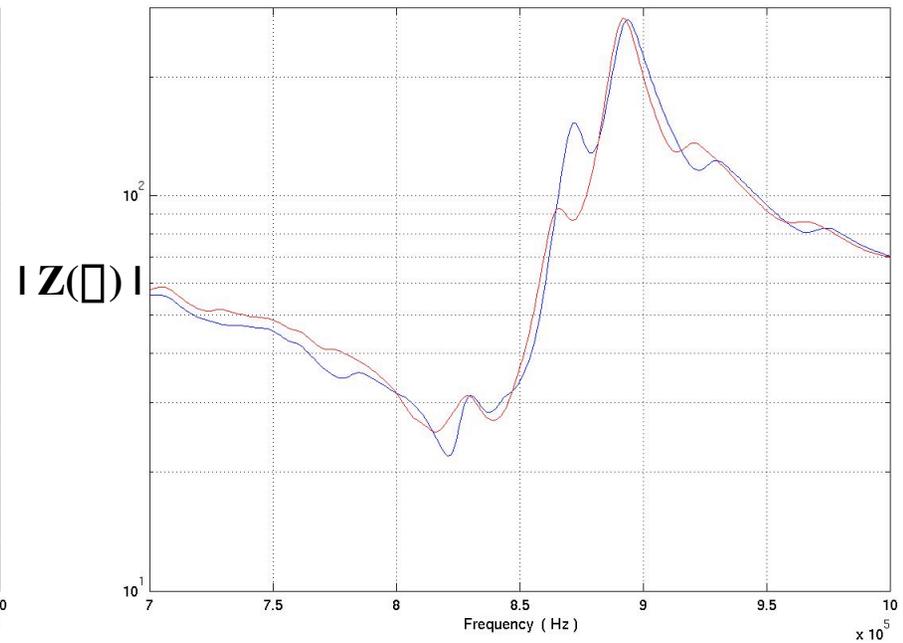
1d Model and 3d Measurements



1d Model



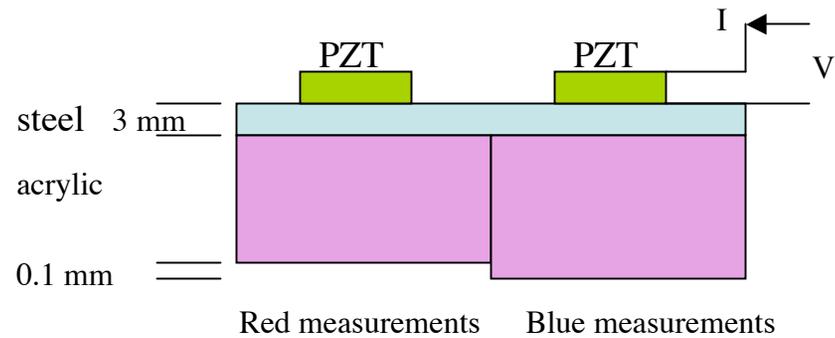
Experiment



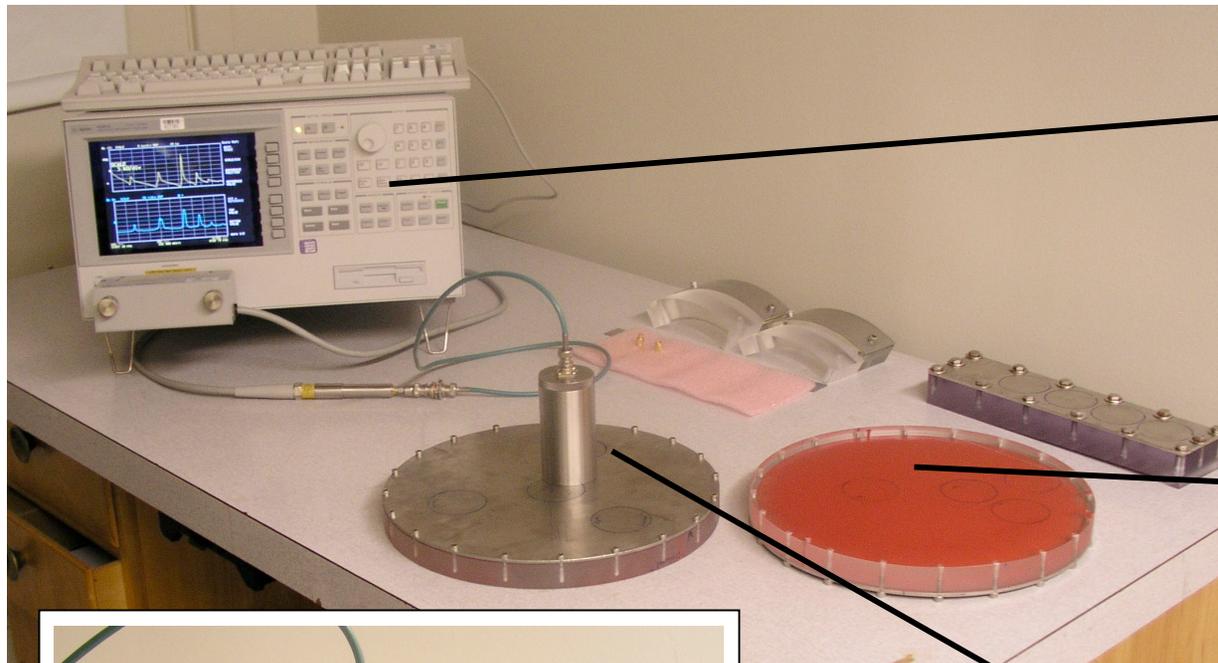
Acrylic Thickness

Blue line : 30.0 mm

Red line : 29.9 mm

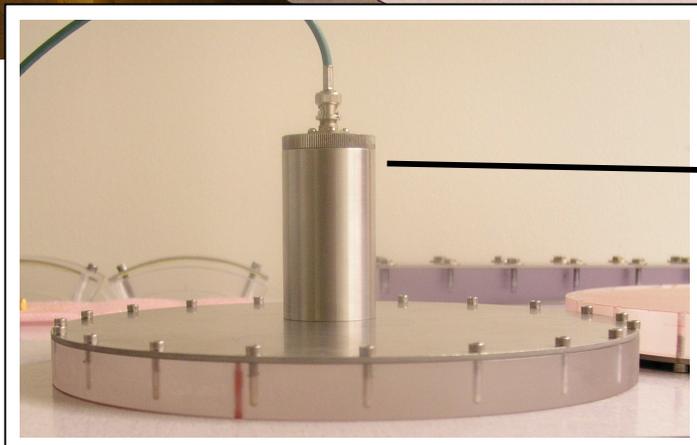


Impedance measurement: consisting of a transducer and a network analyzer



**Agilent 4294A
Impedance analyzer**

Test Phantom (s)

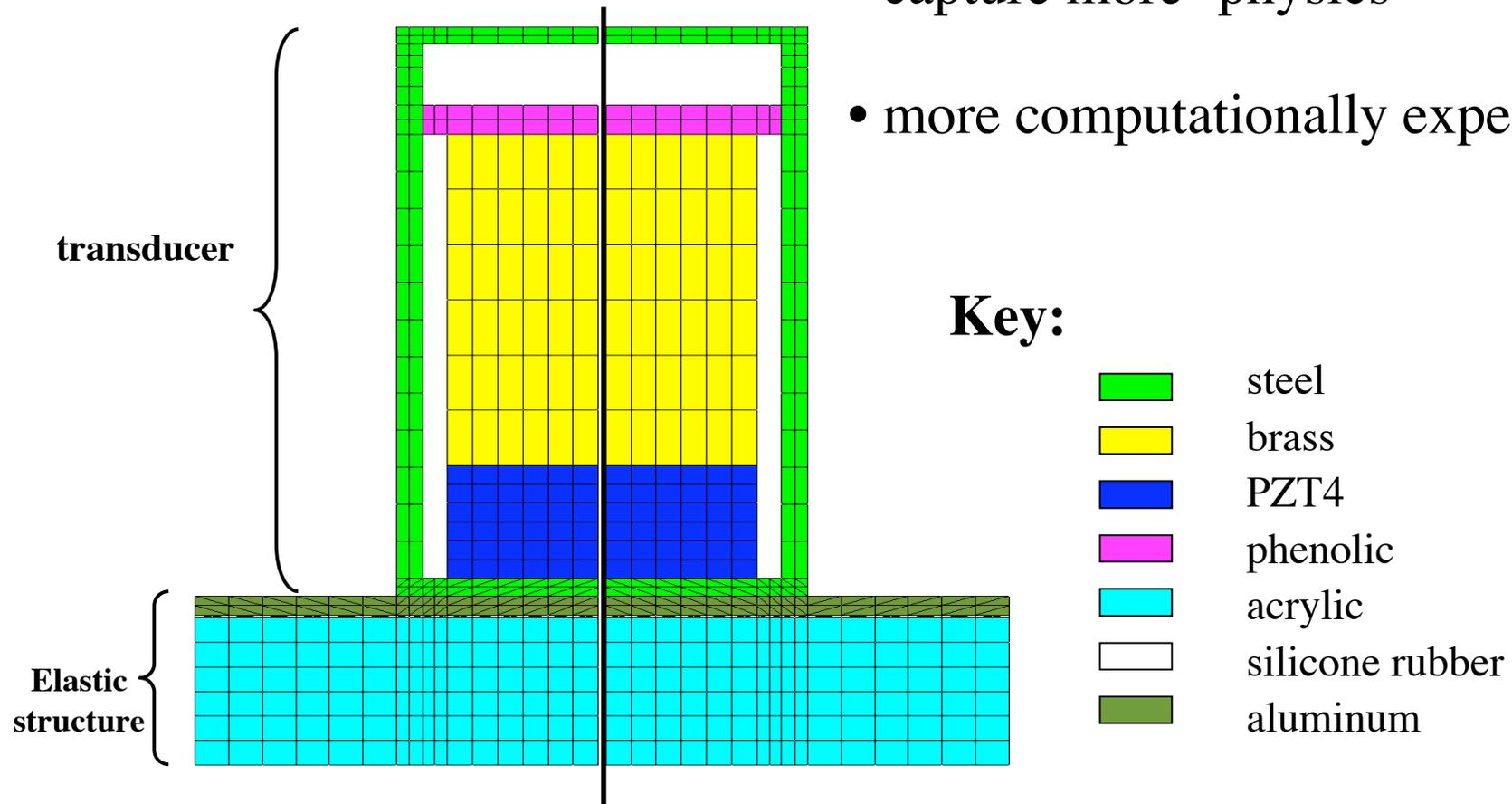


Transducer

2d Axisymmetric Transducer model



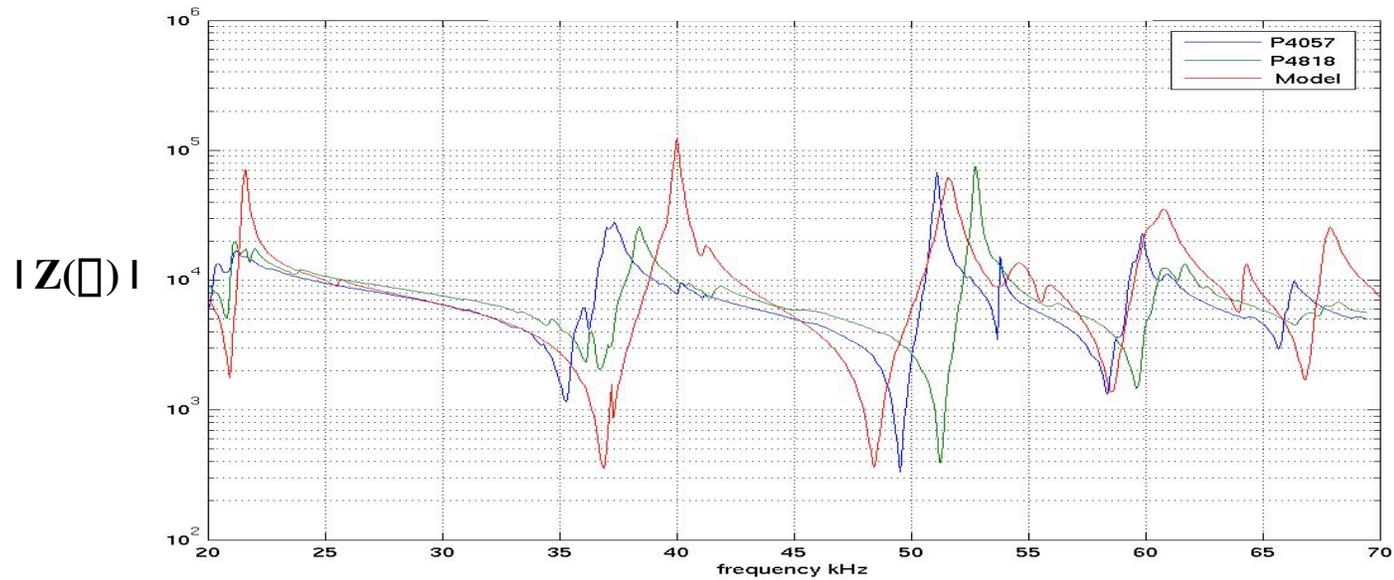
- improved lateral mode model
- capture more 'physics'
- more computationally expensive



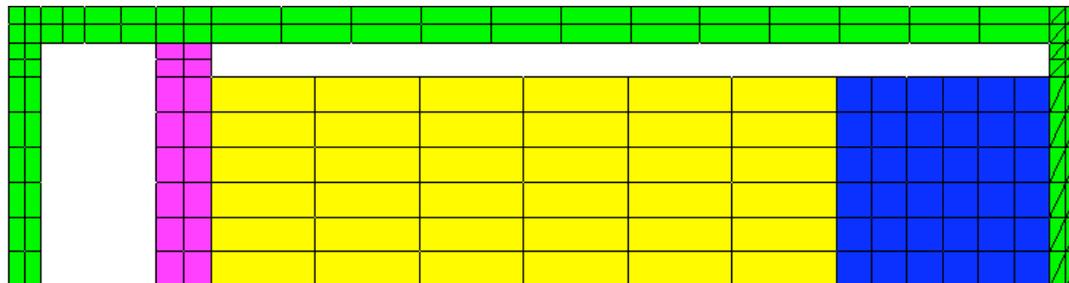
Axi-symmetric Model and Experimental measurements



Transducer Resonances in air



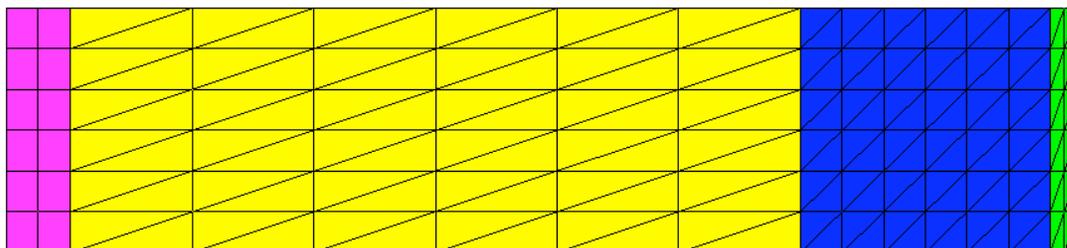
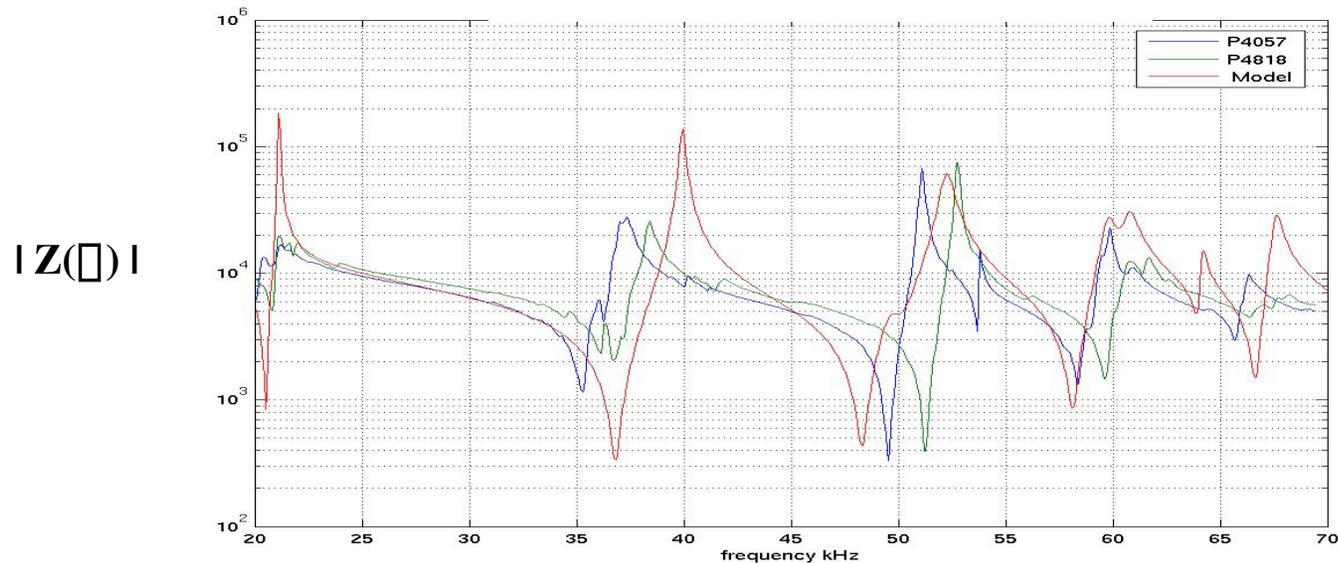
- model
- data set 1
- data set 2



Axi-symmetric Model and Experimental measurements



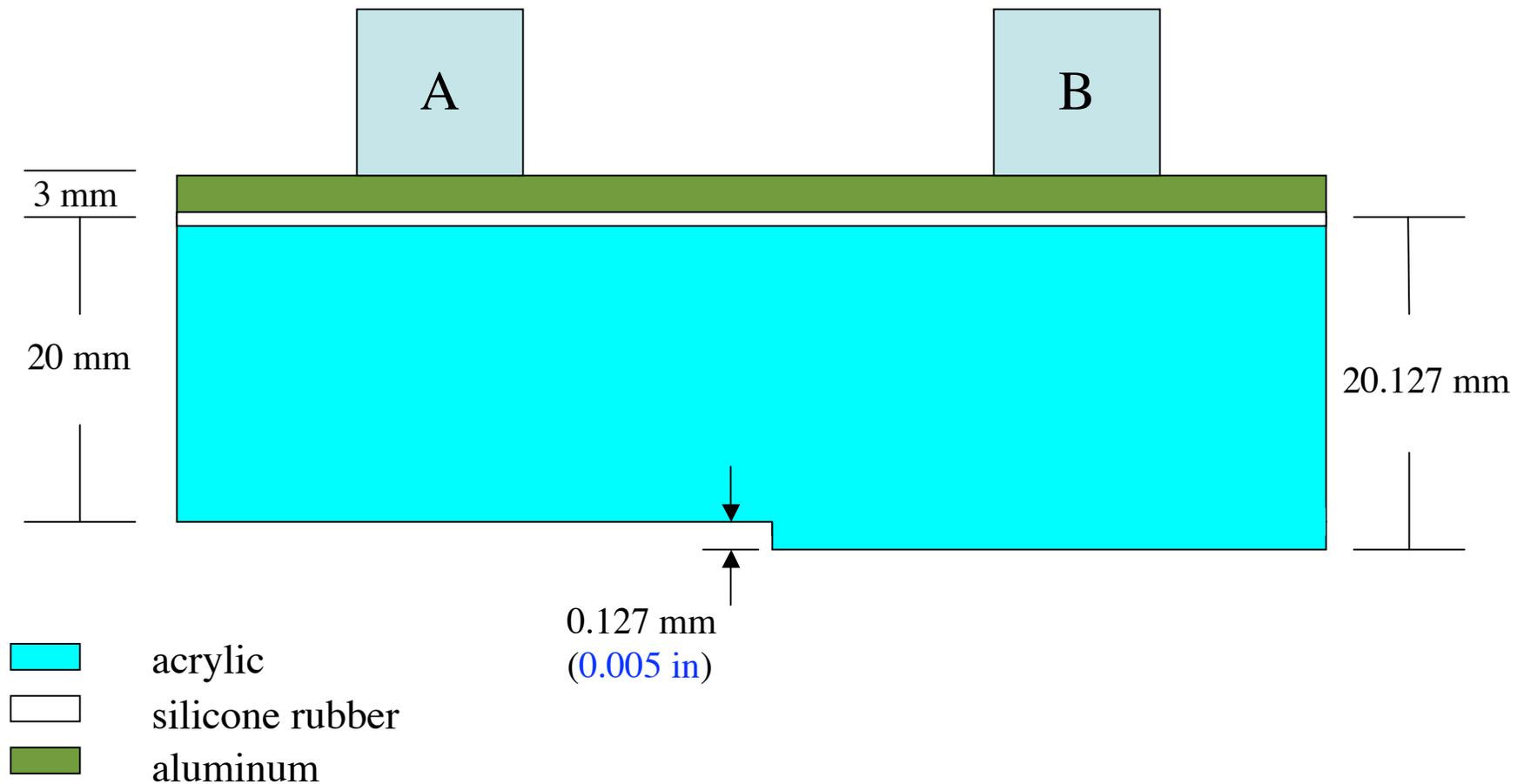
Transducer Resonances in air



Calibrated Step Phantom

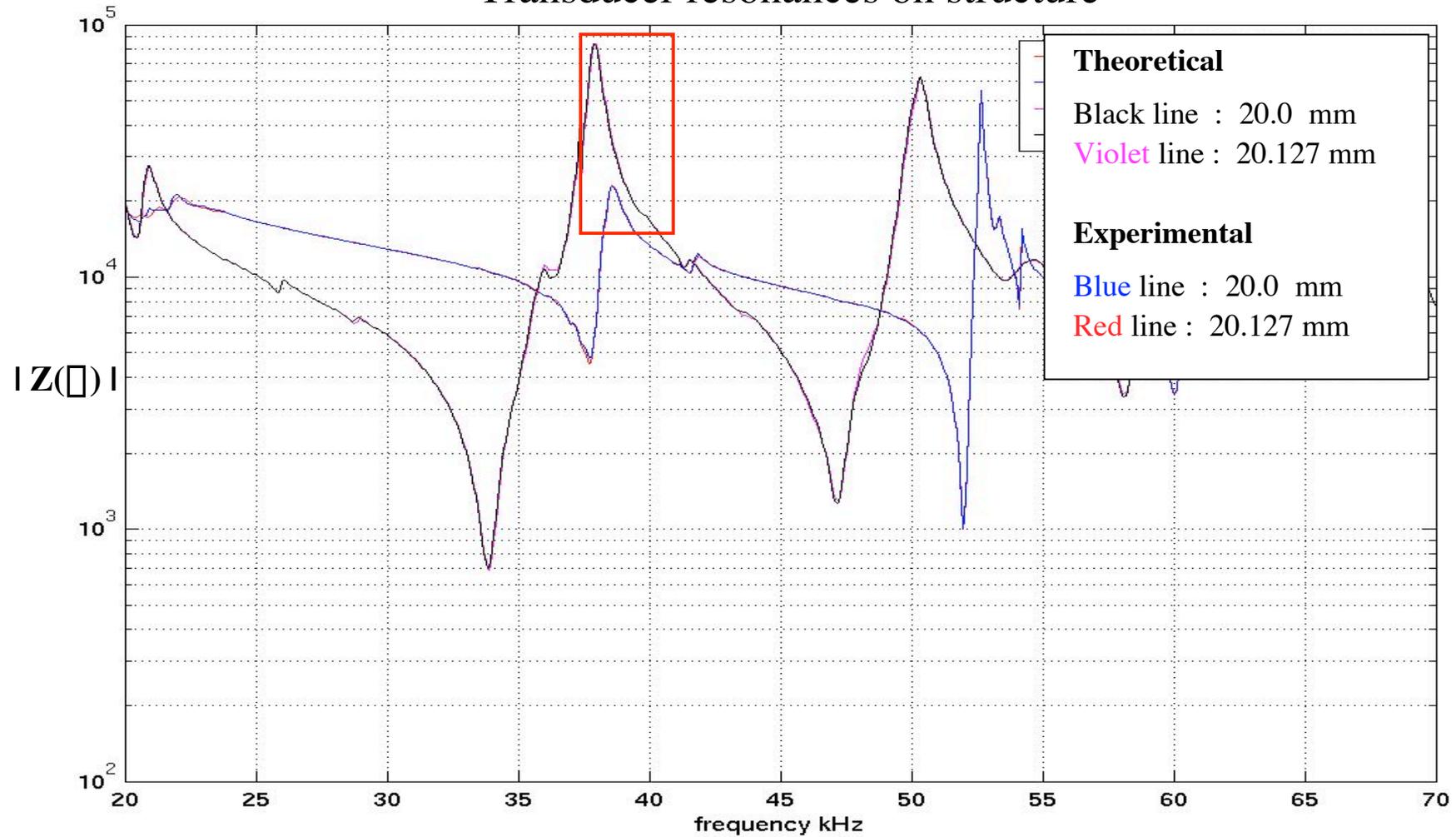


Lower acrylic layer has small step change (0.127 mm) in thickness

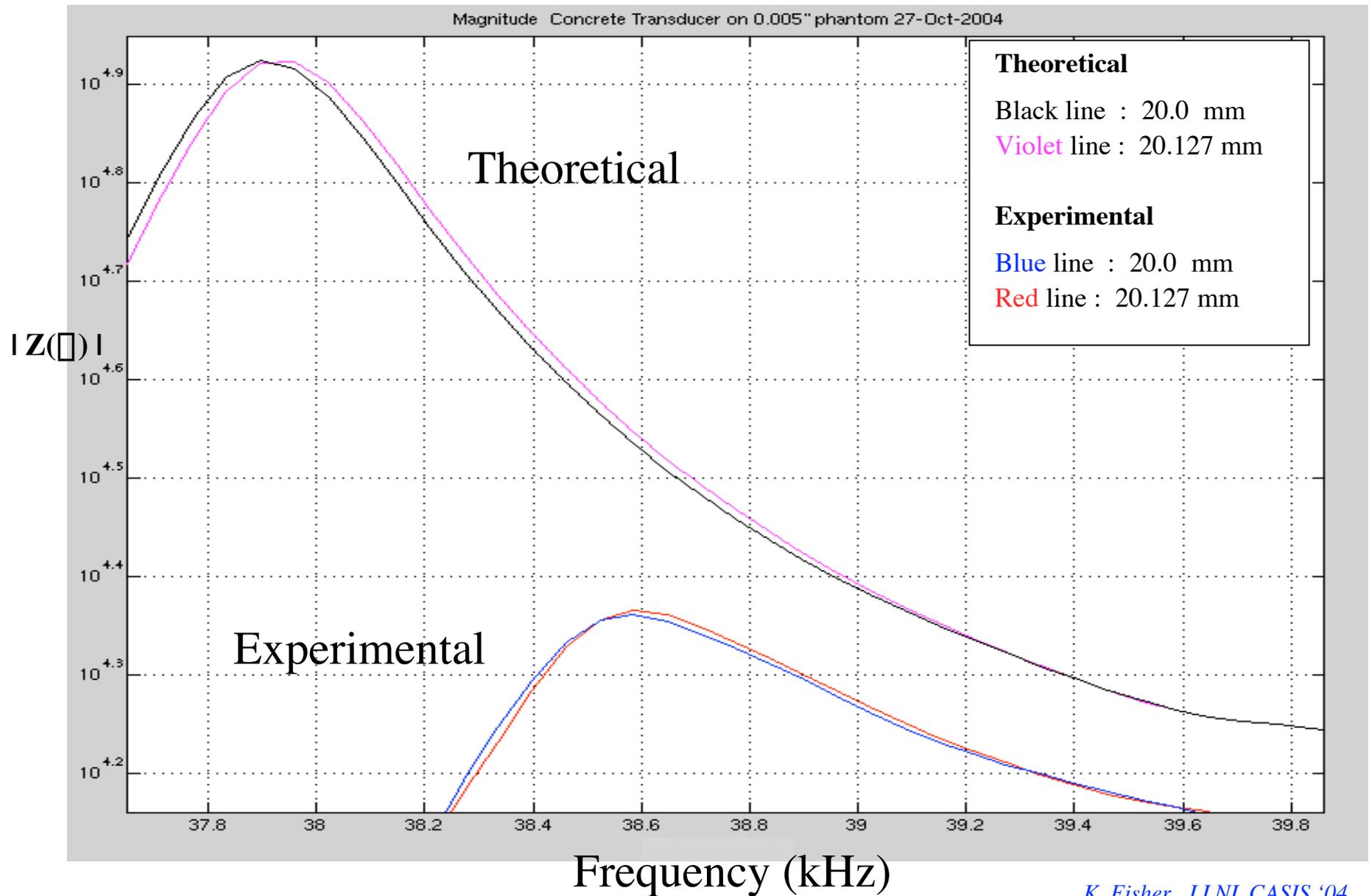




Transducer resonances on structure



Experimental Measurements and Theoretical Predictions





- Develop a robust Impedance Model for the Transducer
- Used as a forward model for an *Inverse Problem*:

Given a measured impedance profile, compute:

- layer thicknesses in multi-layered part
- bulk elastic properties in each layer of part